



Probing exotic structure using one-nucleon transfer reactions

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UNIVERSITY



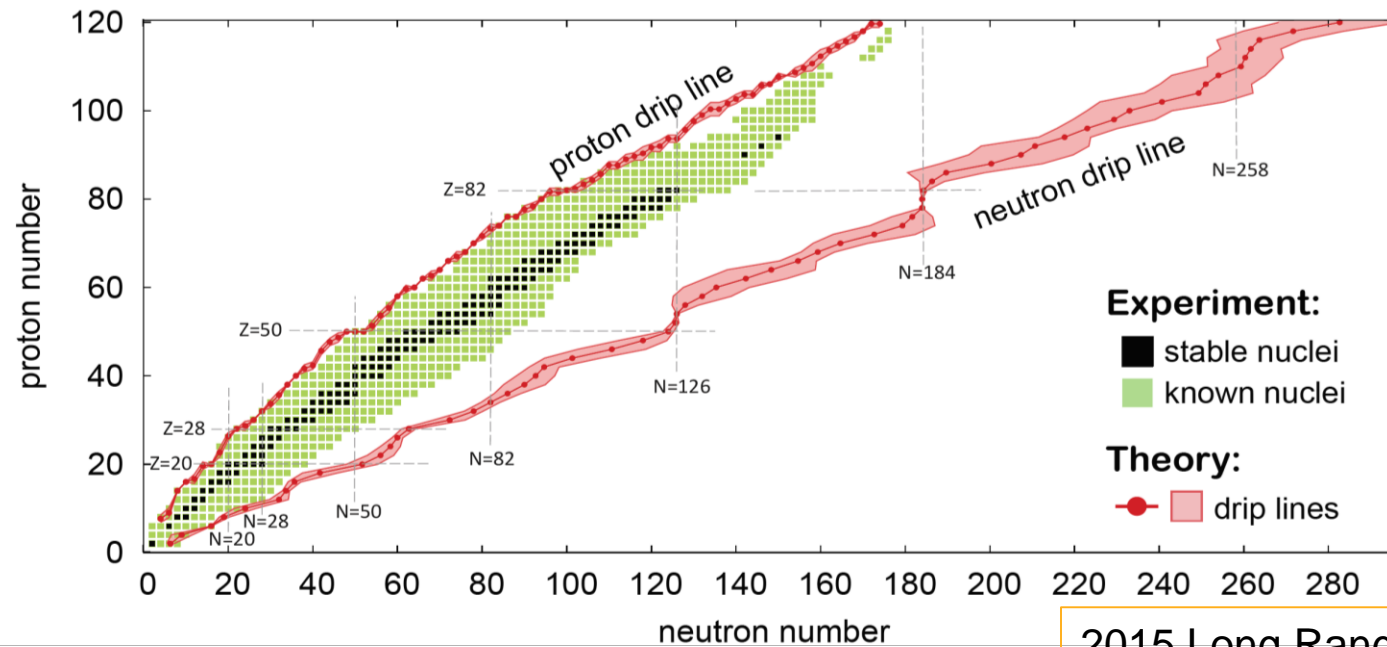
U.S. DEPARTMENT OF
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Science

Outline

- Overarching questions of nuclear physics
 - Migration of shell gaps and magic numbers
- Understanding of exotic nuclei ----- Examples: Be isotopes
 - ^{11}Be negative parity states
 - ^{12}Be intruder states and single-particle configuration mixing
- Resonances in weakly-bound nuclei and the role of continuum
 - ^{12}Be resonances with intruder configurations
- Instrumentation for transfer reactions
- Approaching the nuclear force : N-N effective interaction ----- Example: ^{22}F $1d_{5/2}$ -orbital
- Opportunities with FRIB
 - Commissioning of the AT-TPC and SOLARIS using long-lived beams

Overarching questions of nuclear physics

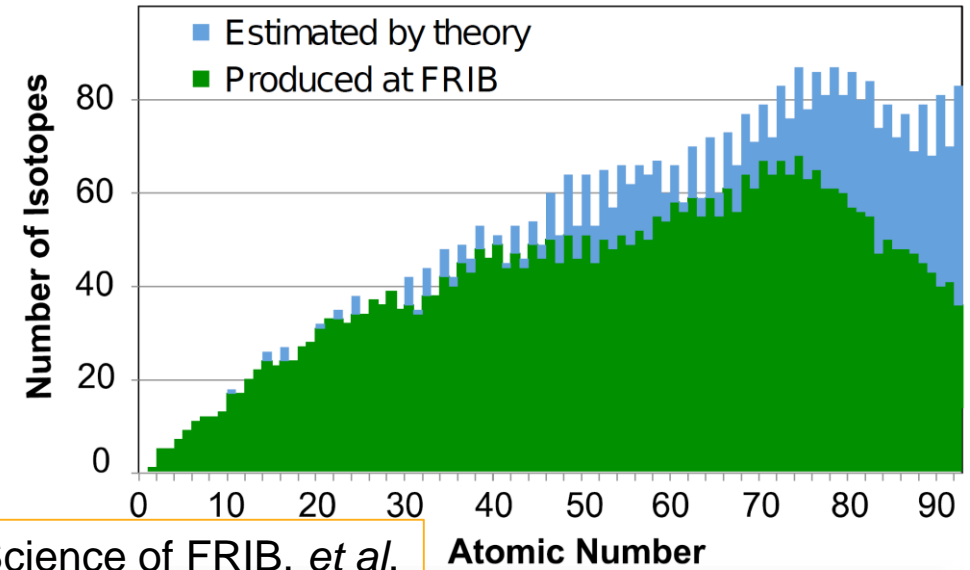


2015 Long Range Plan Reaching for the Horizon <https://science.energy.gov/np/nsac/>.

- Where do nuclei and elements come from?
- What combinations of neutrons and protons can form a bound atomic nucleus?
- New experimental insights on rare nuclei to guide theoretical developments.
- Integration low-energy nuclear experiments and theory with knowledge from astrophysics and computational science.

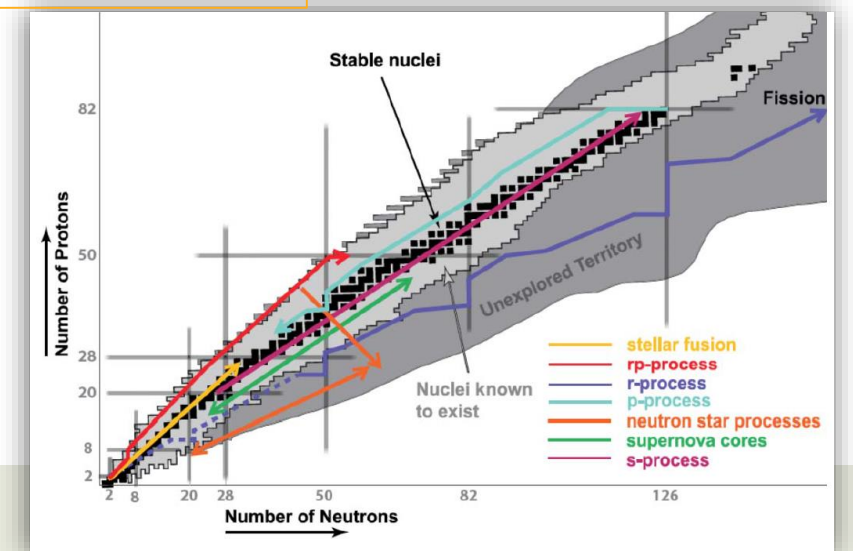
Overarching questions of nuclear physics

- What is the nature of the nuclear force that binds protons and neutrons into stable nuclei and rare isotopes?
- What is the origin of simple patterns in complex nuclei?
- Advanced understanding of the nature of weakly-bound nuclei by measurement of exotic and dripline nuclei
- Determine **shell structure** and test configuration interaction theories
- Measure resonances in weakly-bound nuclei and test the **role of continuum**



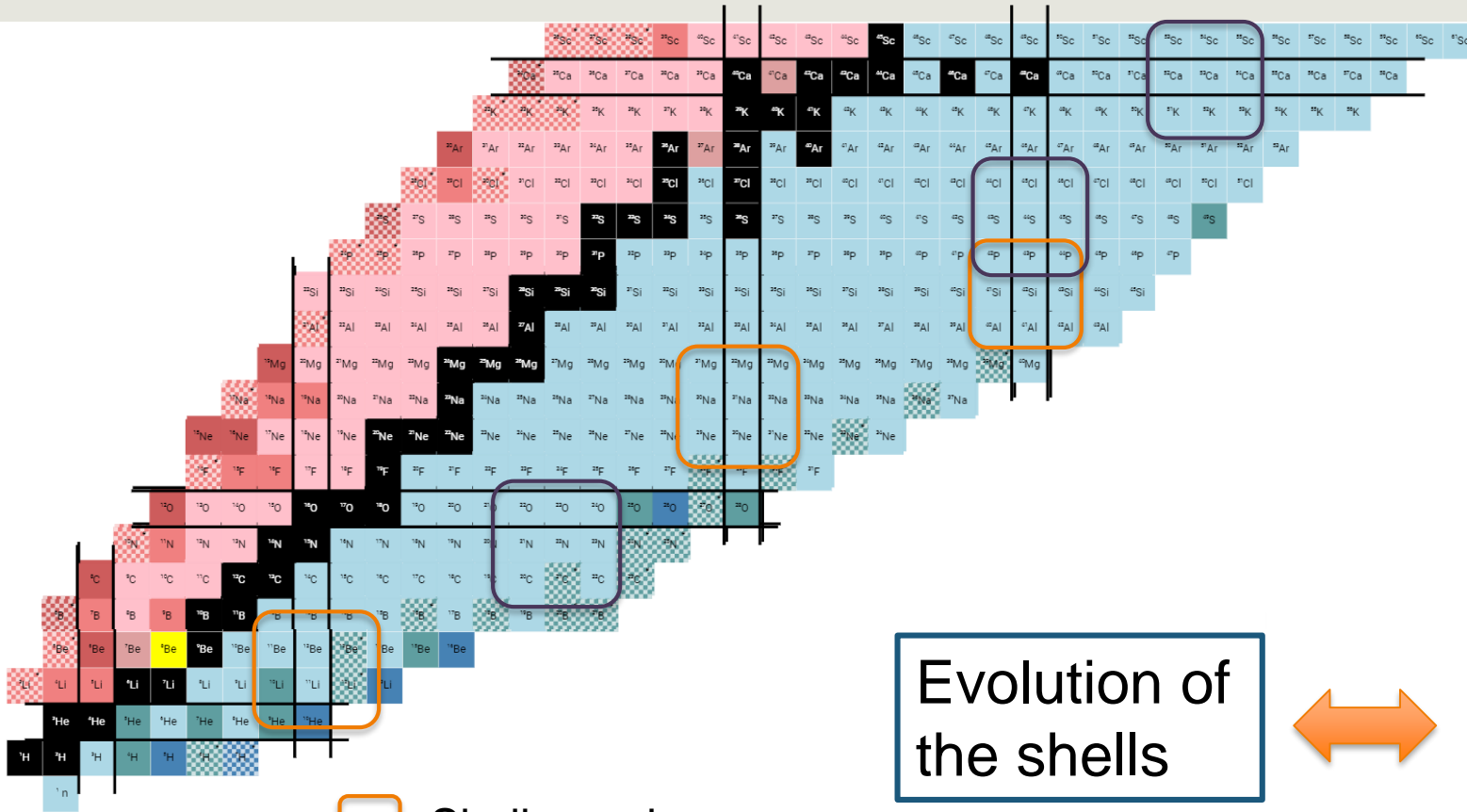
The Science of FRIB, *et al.*

Atomic Number



Jie Chen, Oct. 2020, Postdoc seminar, Slide 4

Migration of Shell Gaps and Magic Numbers

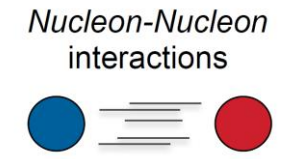


- Shell gap decrease
- Shell gap increase

Evolution of the shells



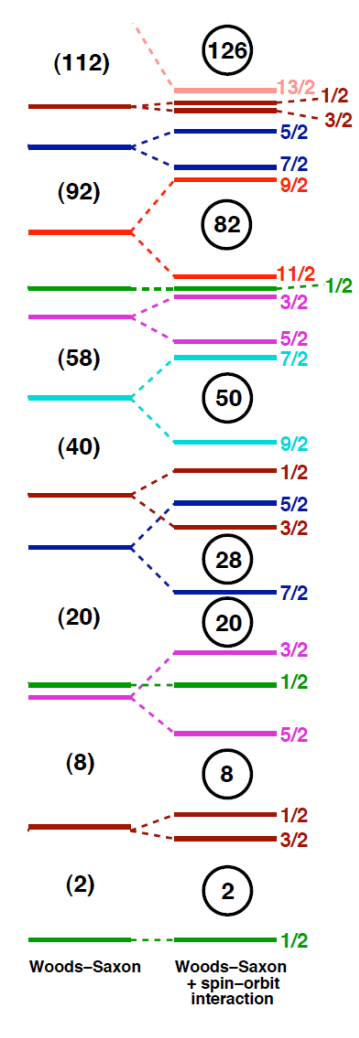
$$\mathcal{E}_i +$$



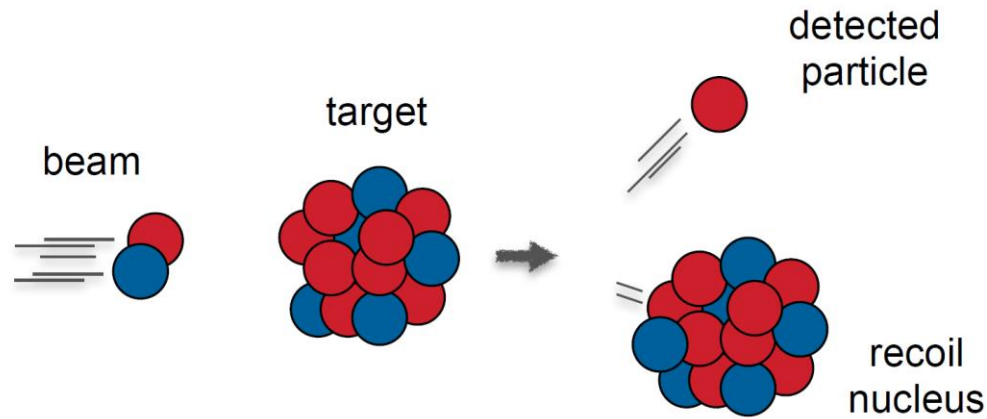
$$V_{ij}^{JT}$$

Effective Single-particle energy

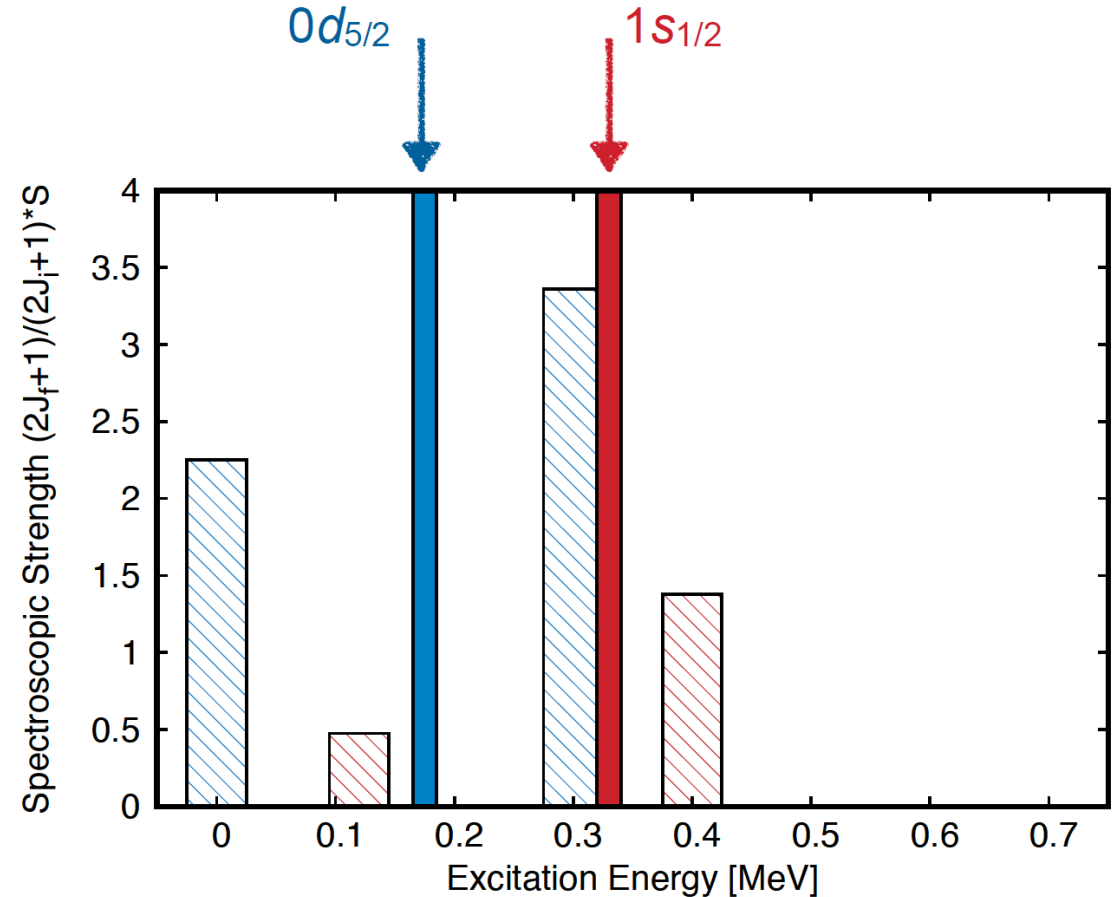
diagonal Terms



Tools to study the evolution of shells / N-N-interaction

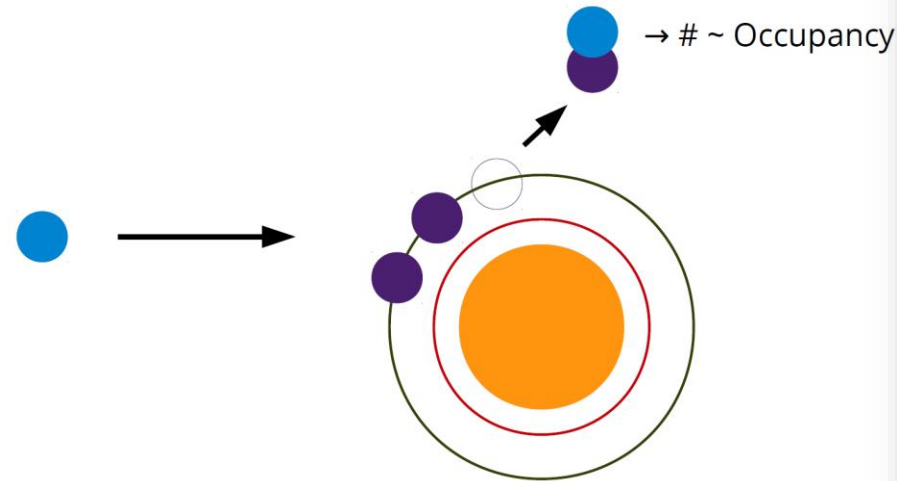


$$E_{centroid} = \frac{\sum (2j_f + 1) S_{lj} * E_{ex}}{\sum (2j_f + 1) S_{lj}}$$



Probing the occupancy and vacancy of the orbitals

- Single-neutron adding probes vacancies (# of holes)
- Single-neutron removal probes occupancies (# of particles)



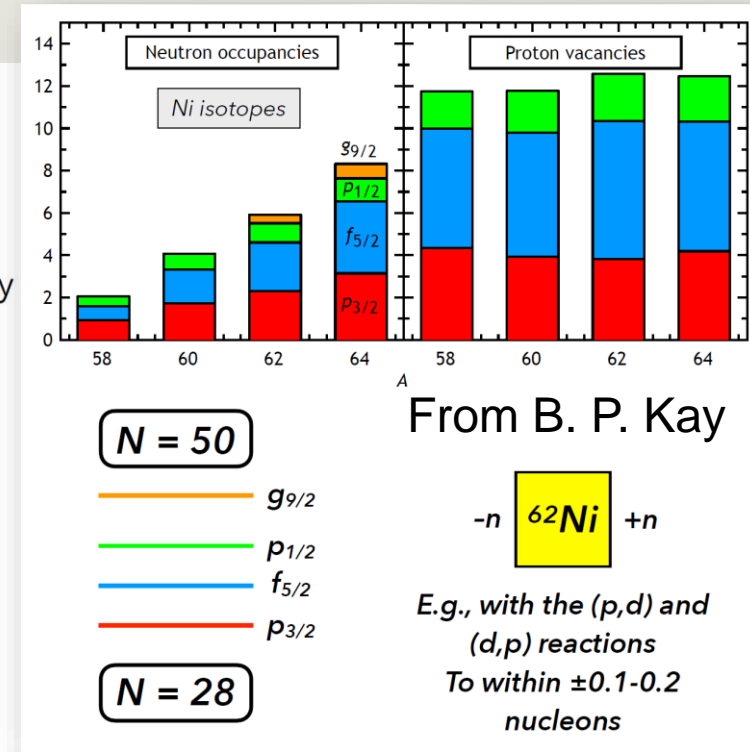
Quenching factor:

$$F_q \equiv \frac{1}{(2j + 1)} \left[\sum \left(\frac{\sigma_{\text{exp}}}{\sigma_{\text{DW}}} \right)_j^{\text{add}} + \sum \left(\frac{\sigma_{\text{exp}}}{\sigma_{\text{DW}}} \right)_j^{\text{rem}} \right],$$

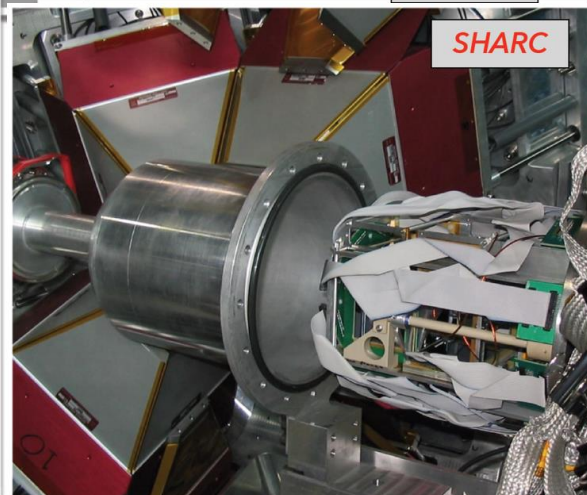
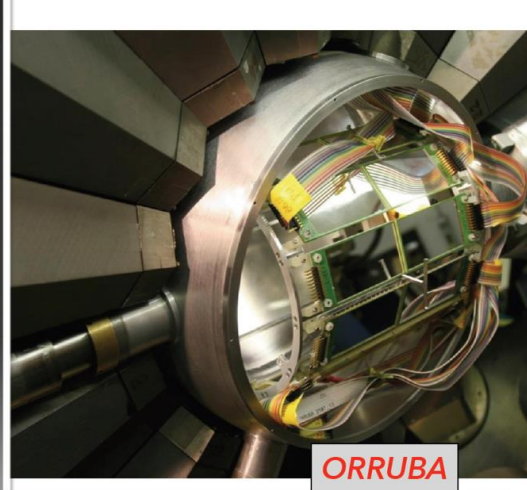
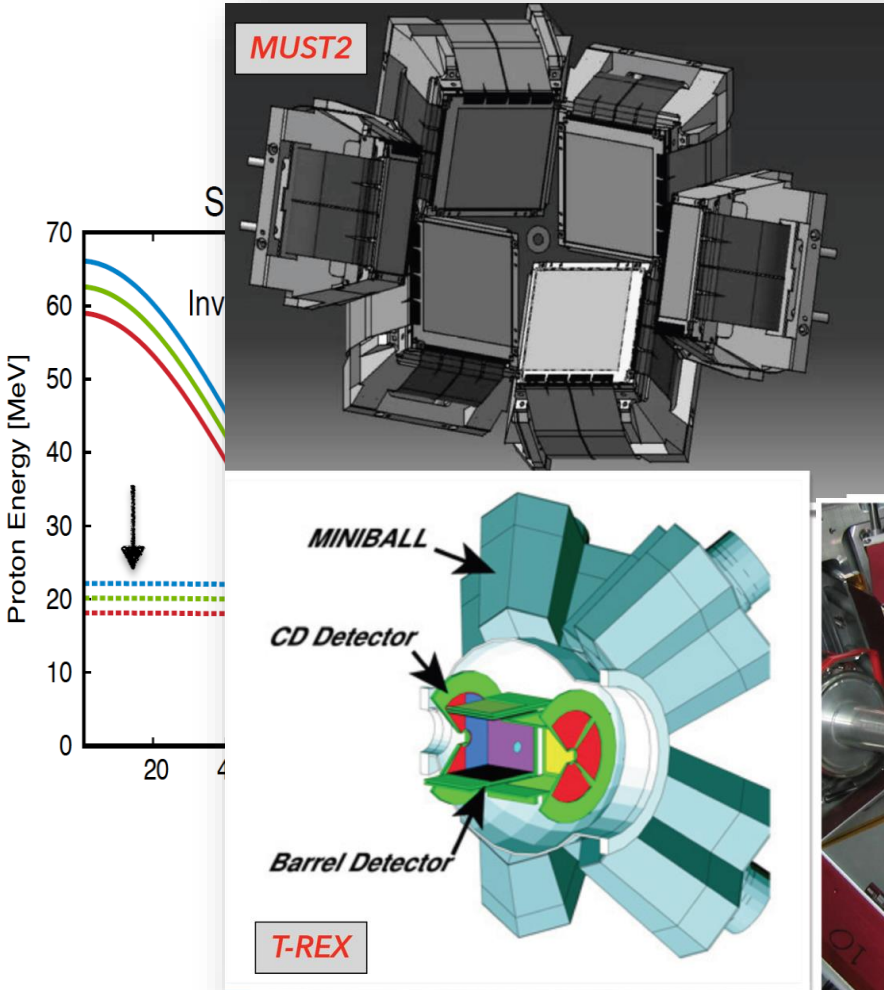
B. P. Kay et. al., PRL 111.042502 (2013)

- Constant value of 0.4~0.7 across all nuclei using consistent optical model parameters
- The Macfarlane-French sum rules can be used to normalize the spectroscopic factors

J. P. Schiffer et. al., PRL 108,022501(2012)



Kinematics: normal vs. inverse



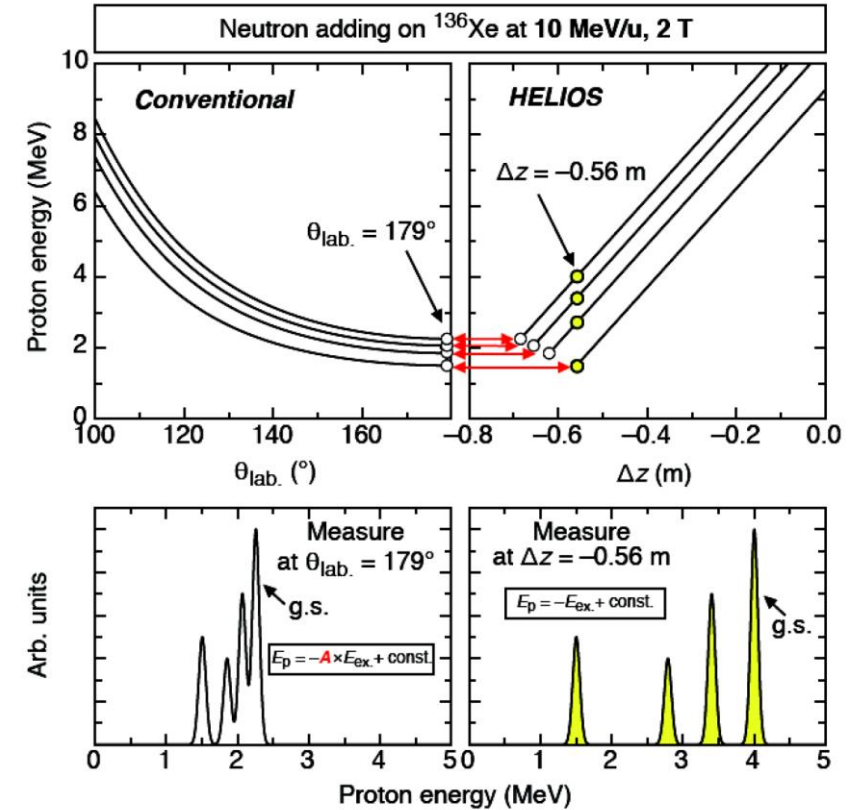
kinematics

low energies

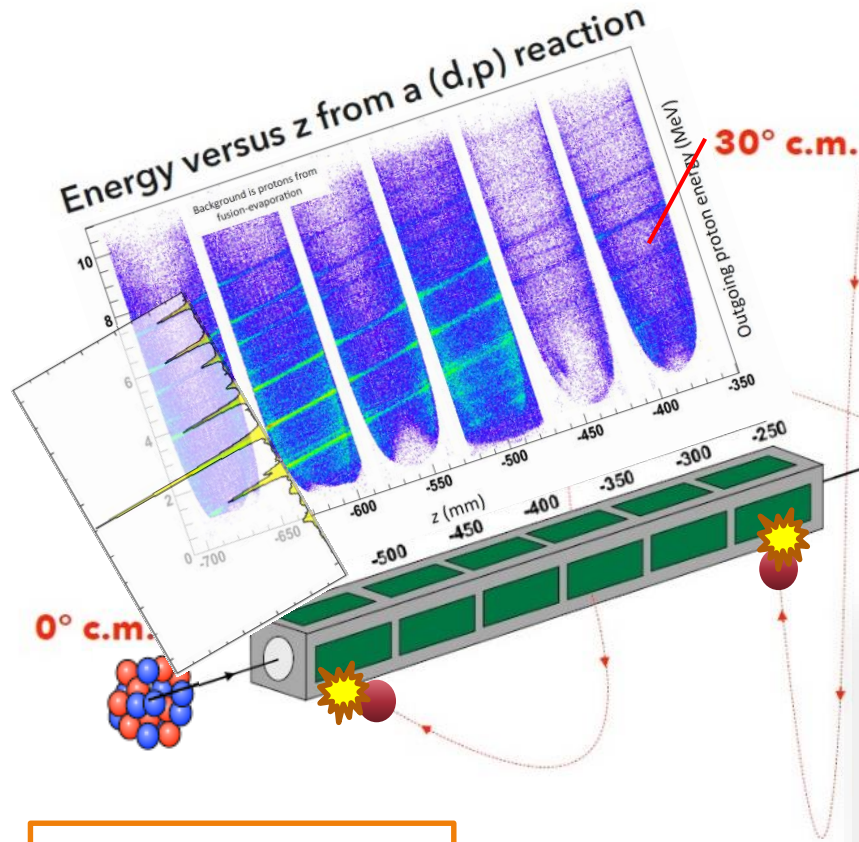
respect to

at forward

resolution



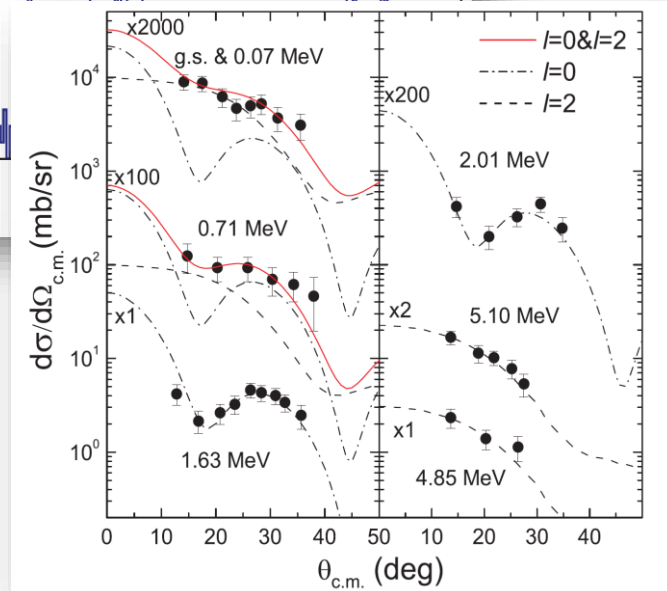
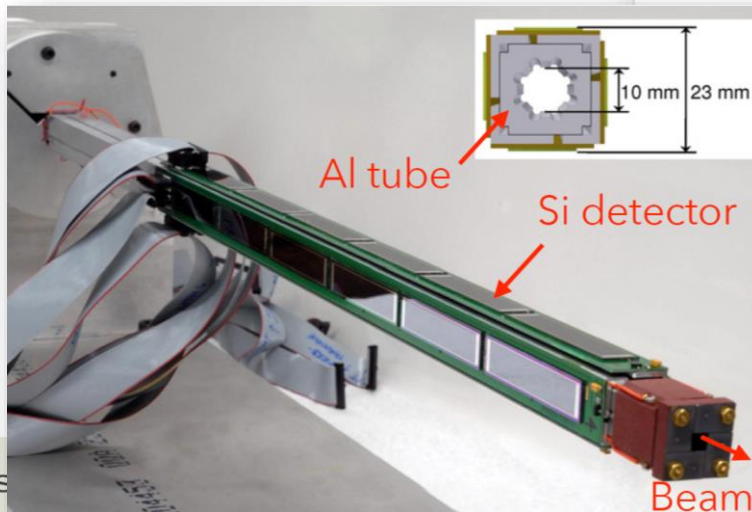
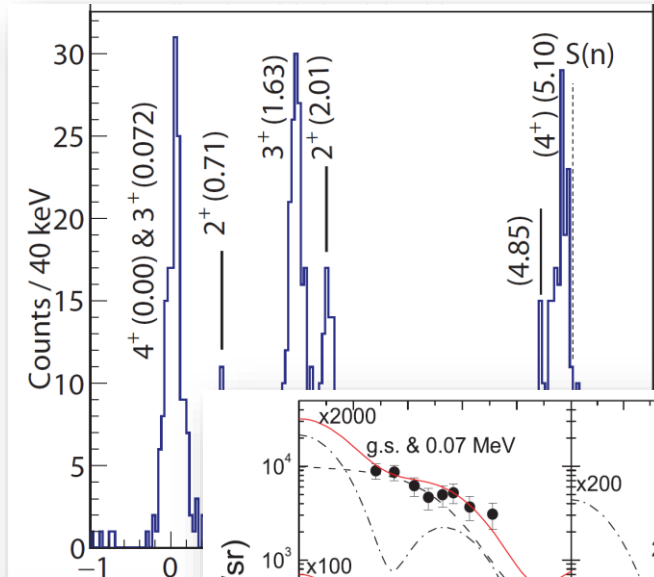
Approaching the nuclear force : N-N effective interaction



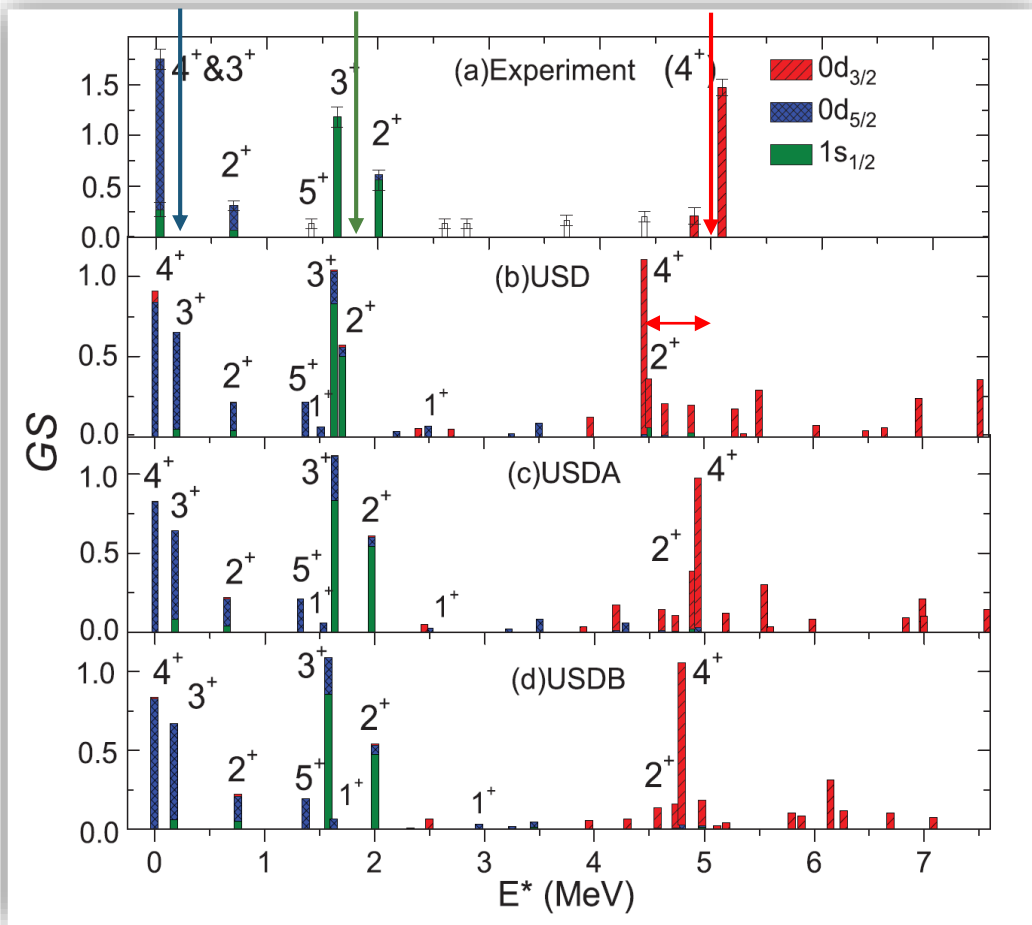
^{21}F 10 A MeV

$^{21}\text{F}(d,p)^{22}\text{F}$

e.g. annular Si detector

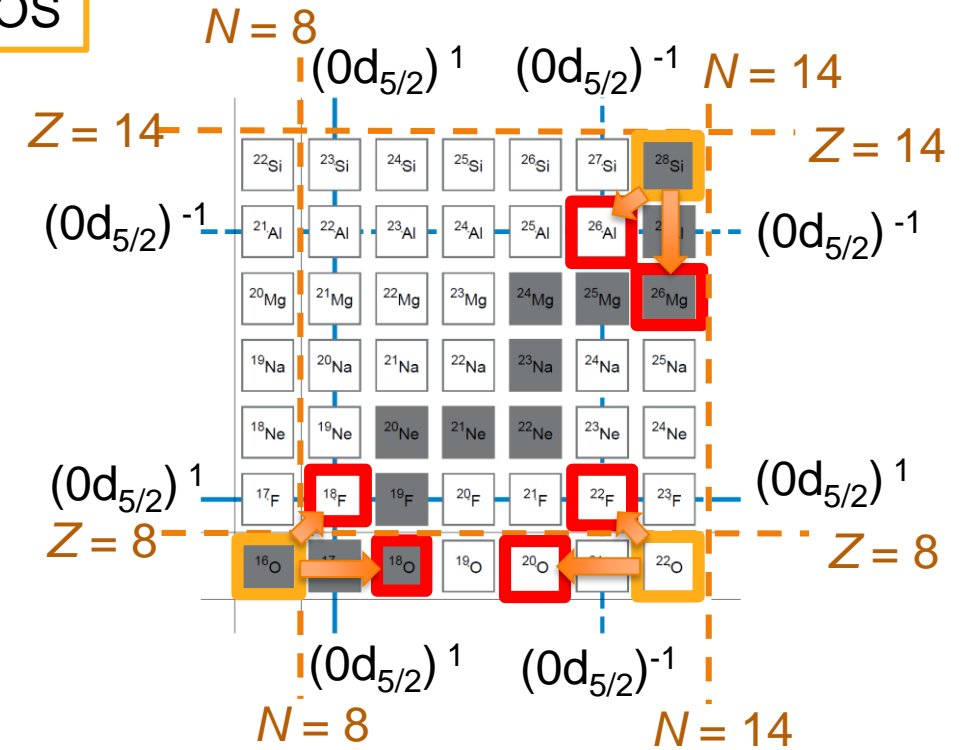


Approaching the nuclear force : N-N effective interaction



$^{21}\text{F}(d,p)^{22}\text{F}$ at 10 MeV/u using HELIOS

Matrix elements in the $1d_{5/2}$ orbital:



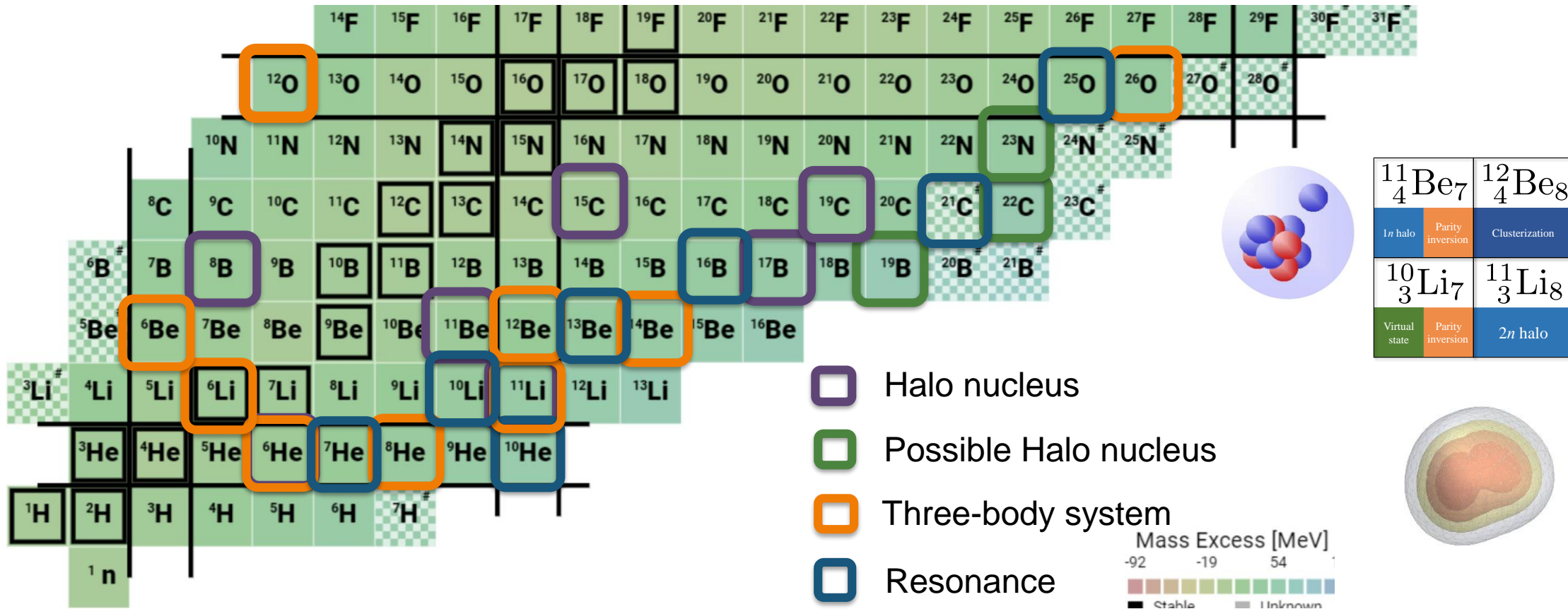
$N=14$ shell gap in ^{22}F : 1.63(6) MeV
Lower limit for $N=16$ shell gap: 3.27(6) MeV

J. Chen *et al.* Phys. Rev. C 98, 014325 (2018)

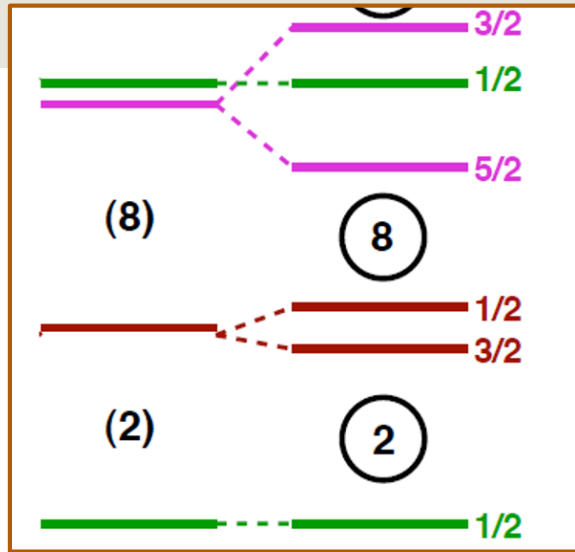


Understanding of exotic nuclei

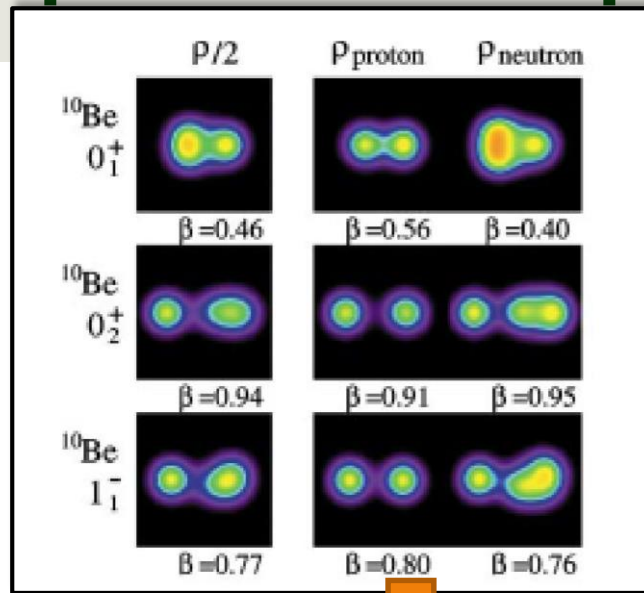
- Halo, Borromean nuclei, three body system, intruder states
- New experimental insights on rare nuclei to challenge theoretical predictions.



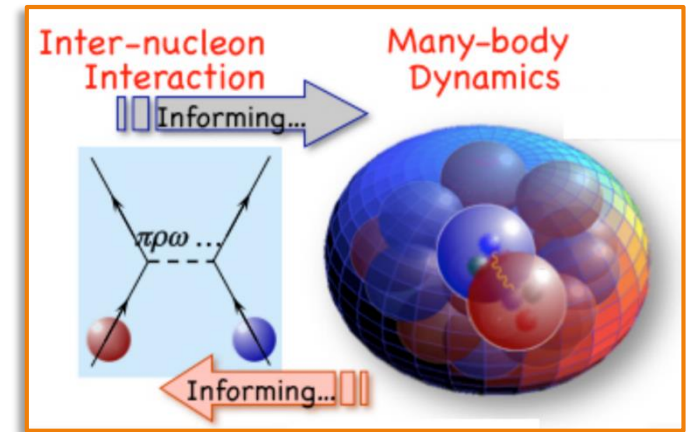
Examples: Be isotopes



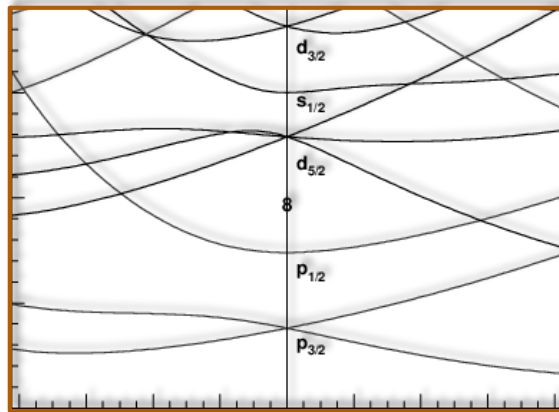
Shell model



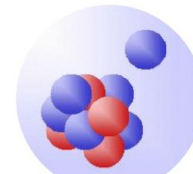
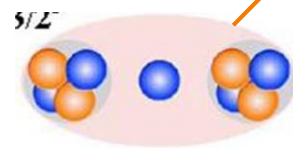
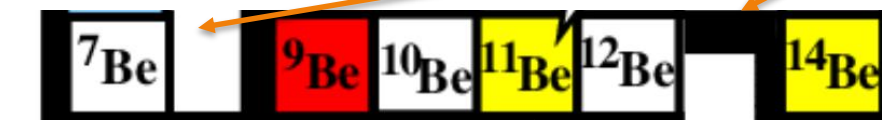
Cluster model



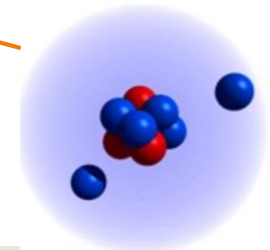
ab-initio method



Nilsson model

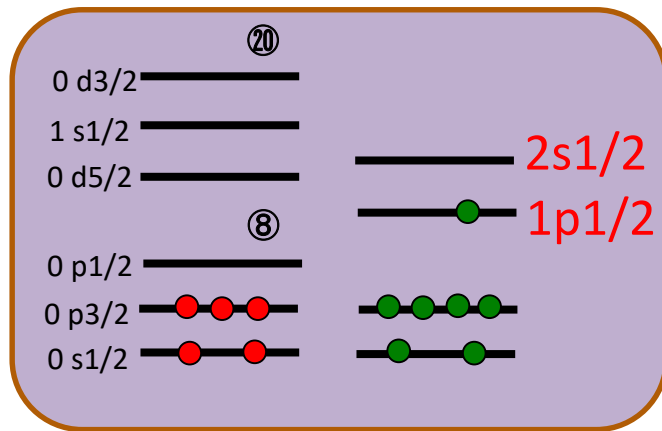


N = 8

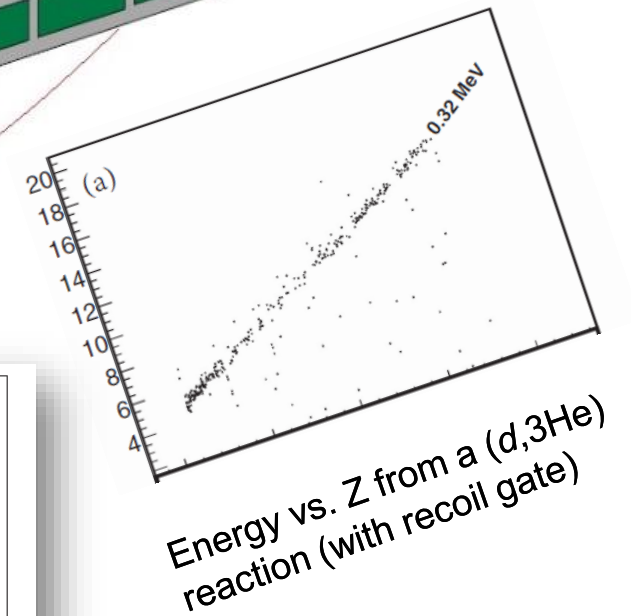
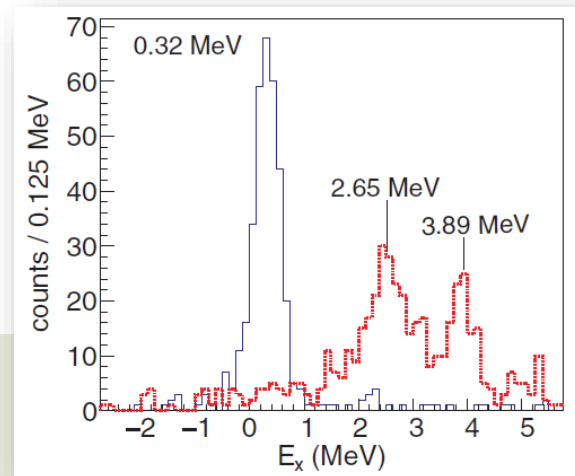
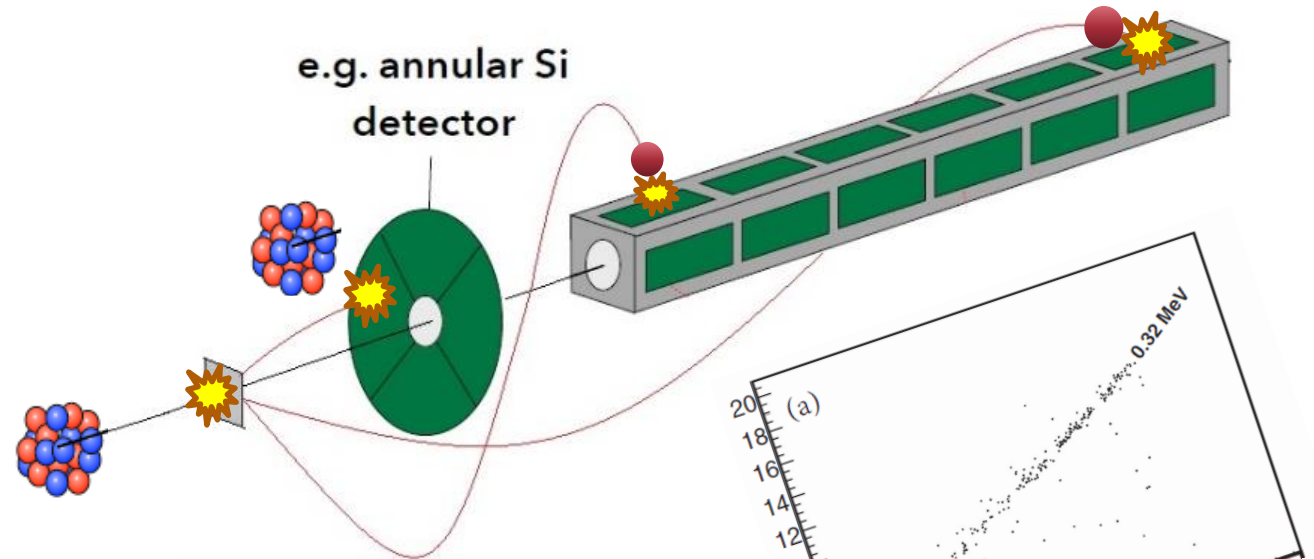


^{11}Be negative parity states

- Neutron loosely bound $S_n = 0.504 \text{ MeV}$
- Larger radius $R = 2.91 \text{ fm}$
- ^{10}Be core + $n(2s_{1/2})$
- g. s. $1/2^+$
- First excited: $1/2^-$



$^{12}\text{B}(d, ^3\text{He})^{11}\text{Be}$

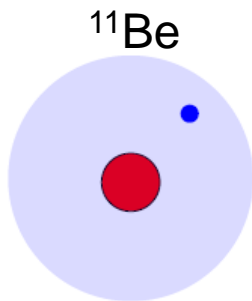


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▪ Testing of various theories

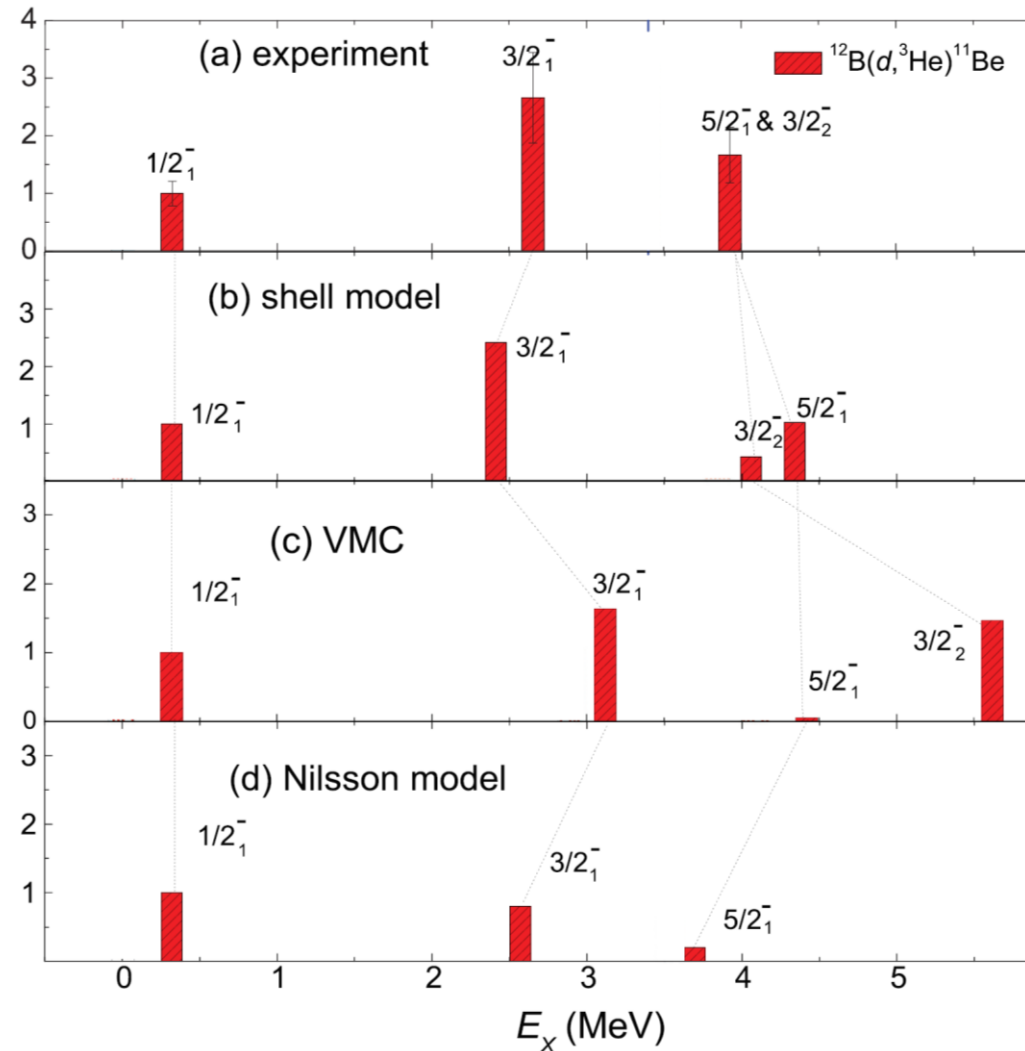
Shell model



Nilsson model

Variational Monte Carlo calculations (VMC)

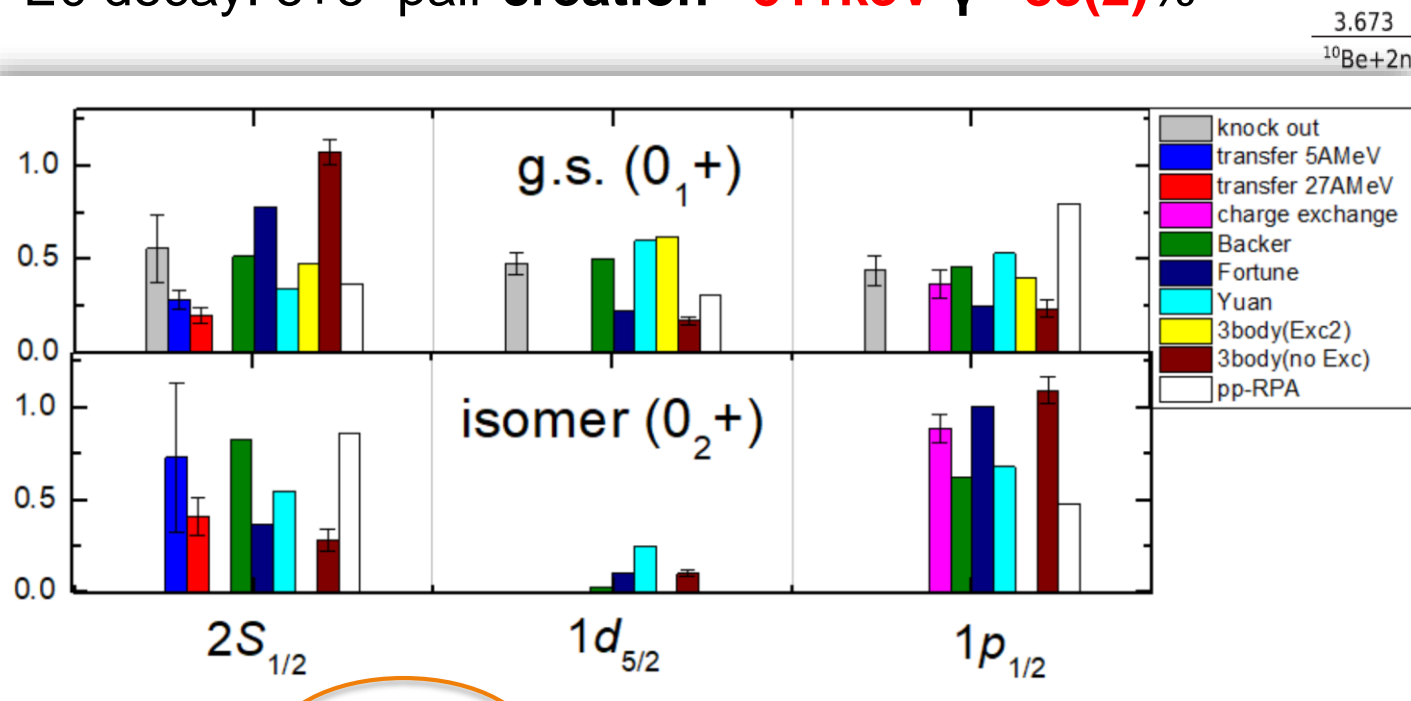
S



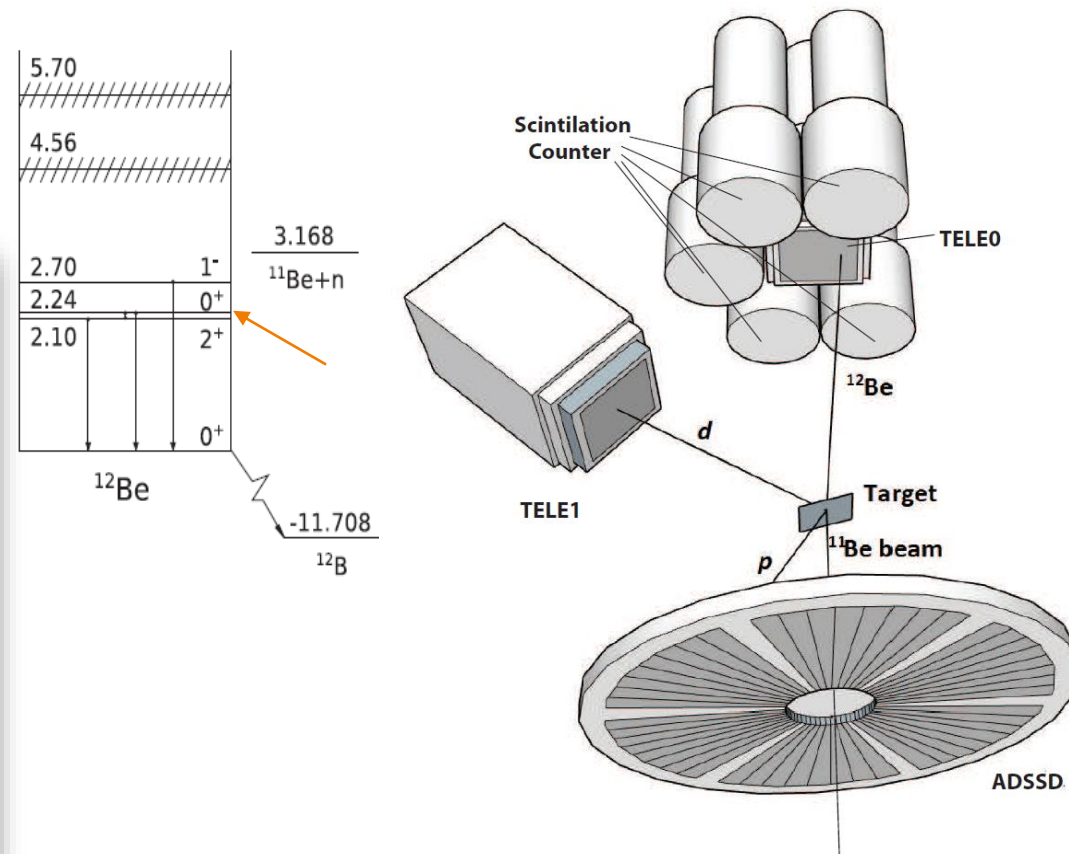
Not a pure strong coupling picture

^{12}Be intruder states and single-particle configuration mixing

- **Breakdown** of conventional magic number: $N=8$
- **Isomeric state**: 0_2^+ 331(12) ns
- E0 decay: $e+e^-$ pair creation **511keV $\gamma \sim 83(2)\%$**

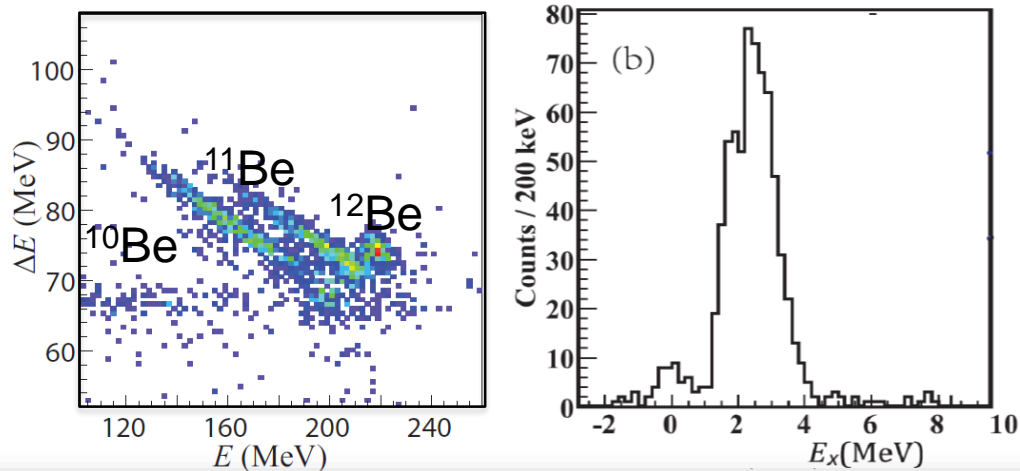


$$|0_i^+\rangle = a_i |1s_{1/2}^2\rangle + b_i |0d_{5/2}^2\rangle + c_i |0p_{1/2}^2\rangle \quad (i = 1, 2)$$



$^{11}\text{Be}(d,p)^{12}\text{Be}$
 J. Chen, J. L. Lou, et al. RCNP E407

^{12}Be intruder states and single-particle configuration mixing



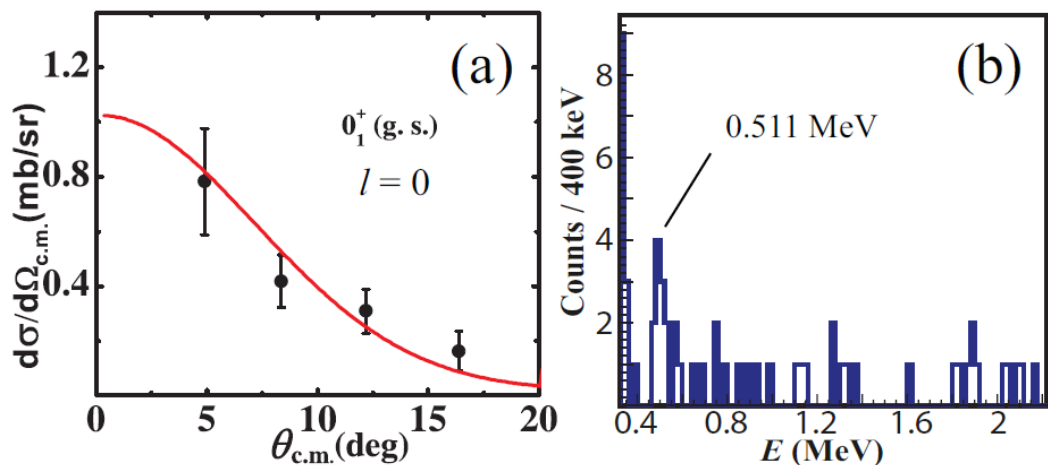
$$|0_i^+\rangle = a_i|1s_{1/2}^2\rangle + b_i|0d_{5/2}^2\rangle + c_i|0p_{1/2}^2\rangle \quad (i = 1, 2)$$

$$a_i^2 + b_i^2 + c_i^2 = \alpha_i + \beta_i + \gamma_i = 1$$

$$a_1 * a_2 + b_1 * b_2 + c_1 * c_2 = 0$$

Ratio of $2s_{1/2}$ intensity: $\alpha_1/\alpha_2 = 0.20/0.41 = 0.49^{+0.15}_{-0.16}$

charge-exchange : $\gamma_1 = 0.24$ and $\gamma_2 = 0.59$

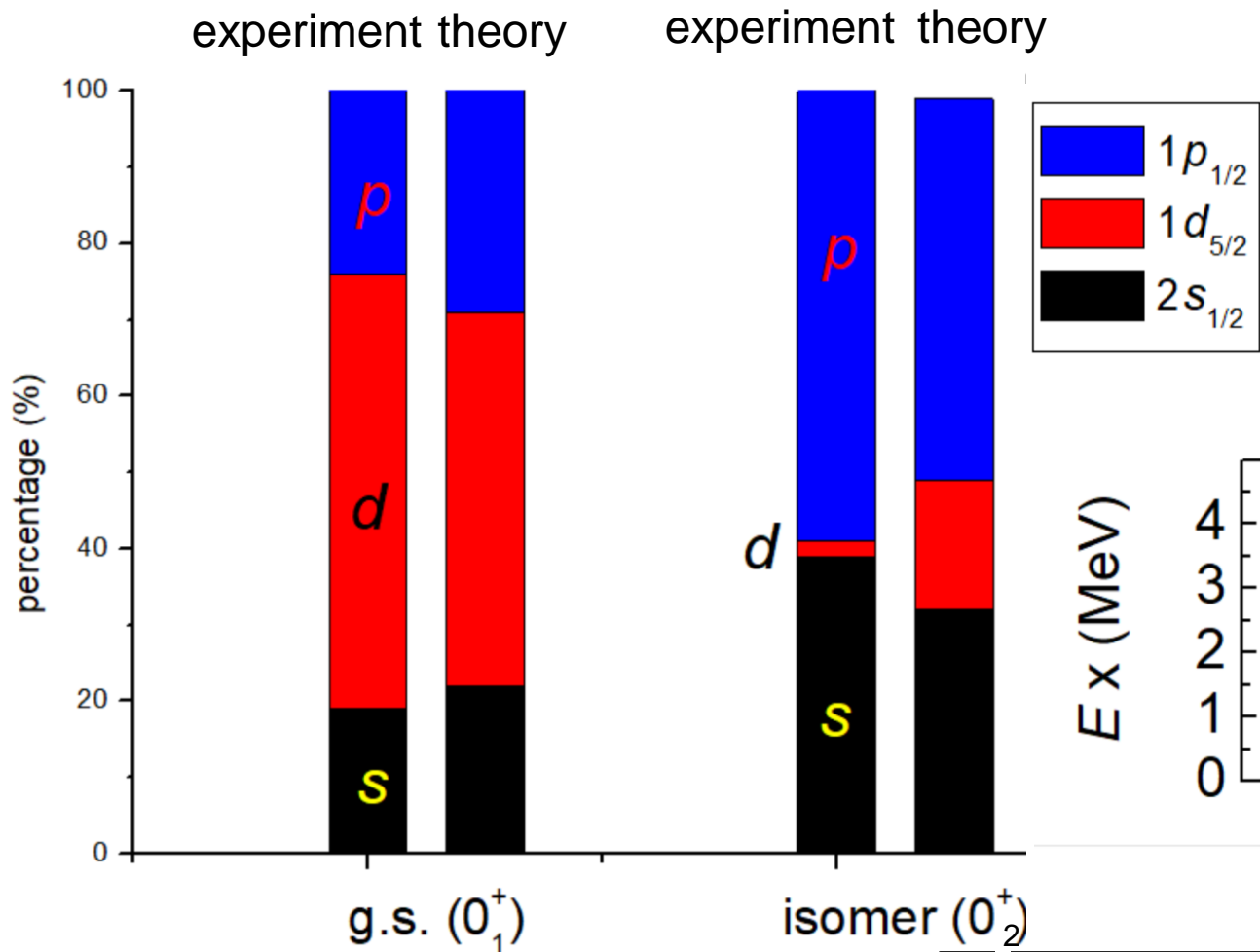


ADWA calculation

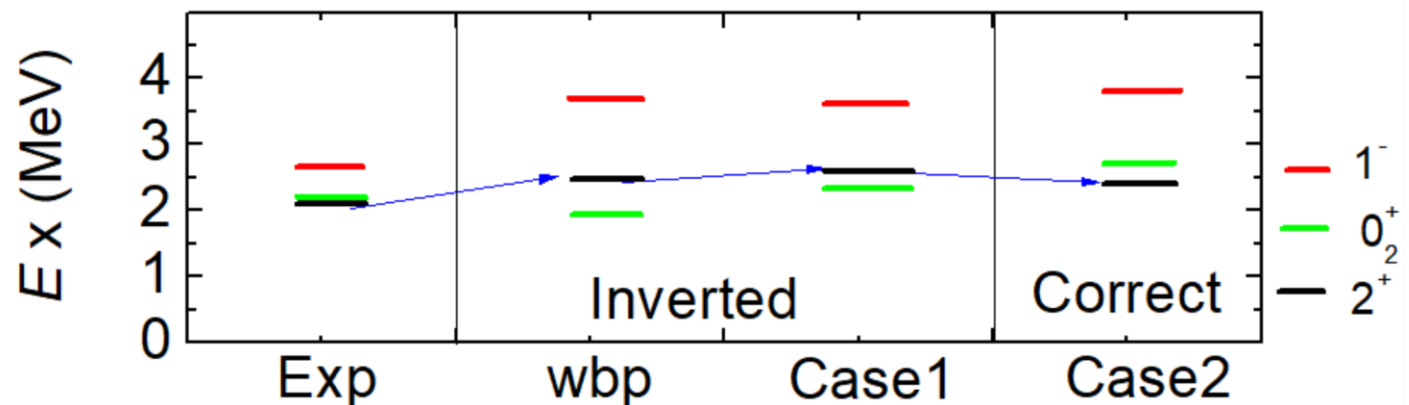
0_1^+			0_2^+		
$\alpha_1(\%)$	$\beta_1(\%)$	$\gamma_1(\%)$	$\alpha_2(\%)$	$\beta_2(\%)$	$\gamma_2(\%)$
($2s_{1/2}$)	($1d_{5/2}$)	($1p_{1/2}$)	($2s_{1/2}$)	($1d_{5/2}$)	($1p_{1/2}$)
19 ± 7	57 ± 7		39 ± 2	2 ± 2	

■ Quenching Factor: $F_q = \frac{SF_{\text{exp}}}{I(2j+1)} = 0.55(10)$

^{12}Be intruder states and single-particle configuration mixing



- The g. s. of ^{12}Be is dominated by a d -wave intruder configuration
- Dramatic change compared to ^{11}Be
- Possibly due to stronger pairing in $d_{5/2}$ -orbital
- Deformation lowered $d_{5/2}$ -orbital energy



J. Chen *et al.* Phys. Lett. B 781 (2018) 412 - 416
 J. Chen *et al.* Phys. Rev. C 98, 014616 (2018)

J. Chen *et al.* Phys. Rev. C 94, 064620 (2016)
 J. Chen *et al.* Phys. Rev. C 93, 034623 (2016)

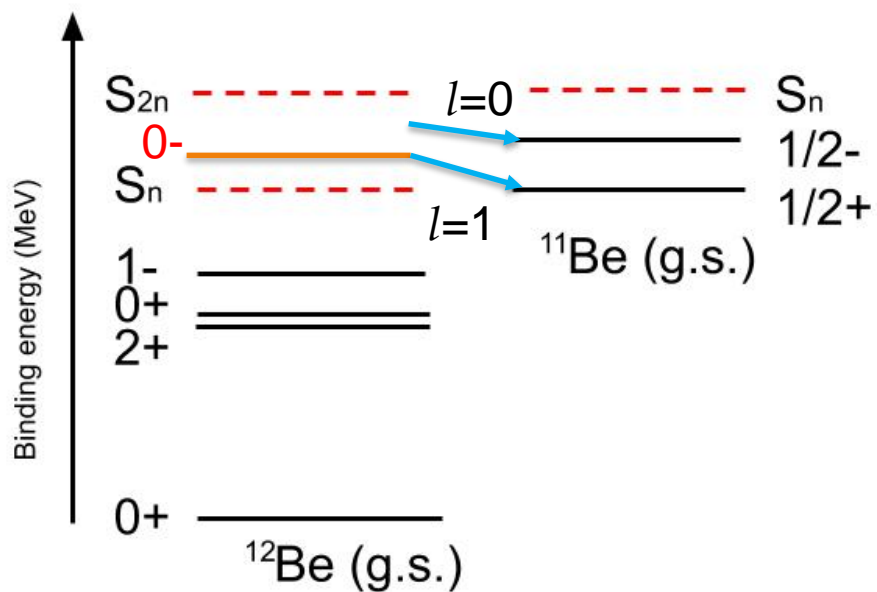
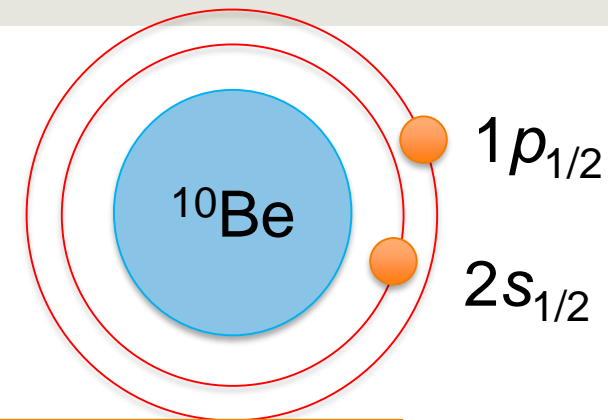


Outline

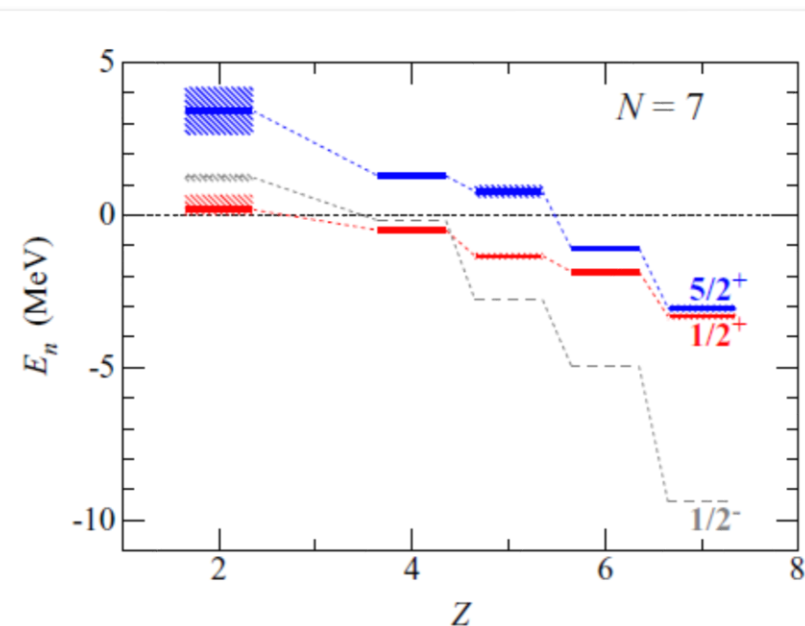
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 - Migration of Shell Gaps and Magic Numbers
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 - ^{11}Be negative parity states
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- Resonances in weakly-bound nuclei and the role of continuum
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^{12}Be unbound states

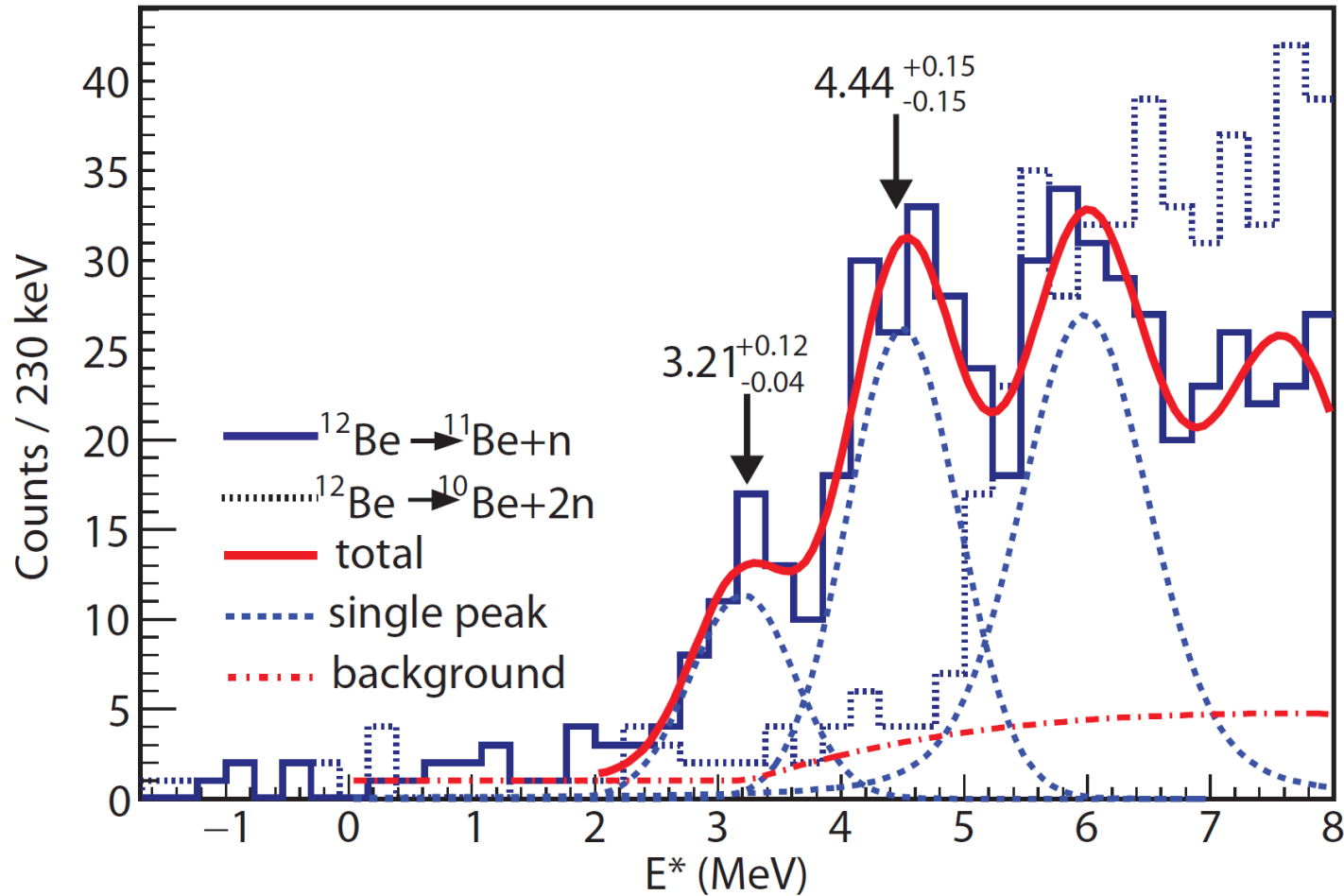
- Breakdown of $N=8$ \longleftrightarrow 1p-1h across the $N=8$
- Neutrons in $2s_{1/2}$ and $1p_{1/2}$ \longleftrightarrow 1- and 0- states
- Previous measurements ruled out a bound 0- state



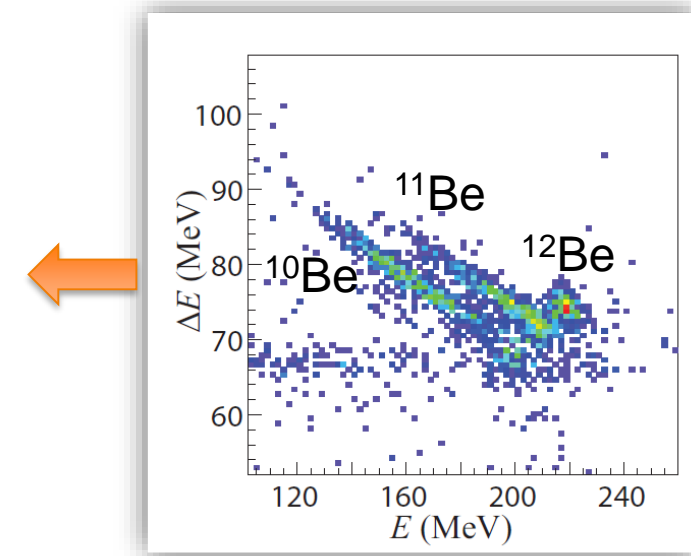
Convenient location of the 0- state



^{12}Be unbound states

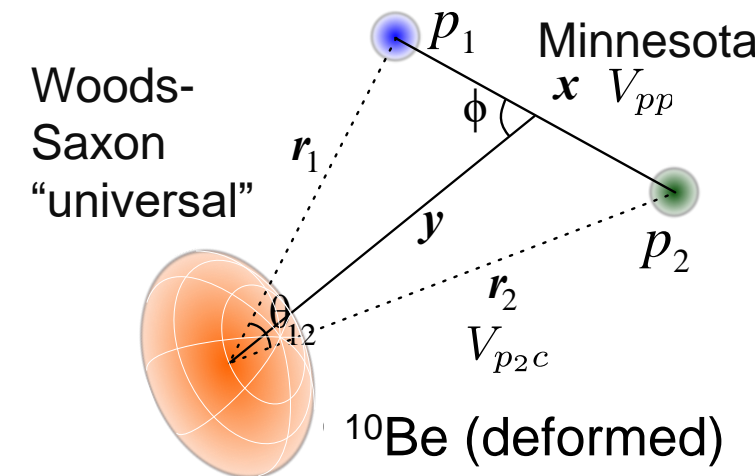
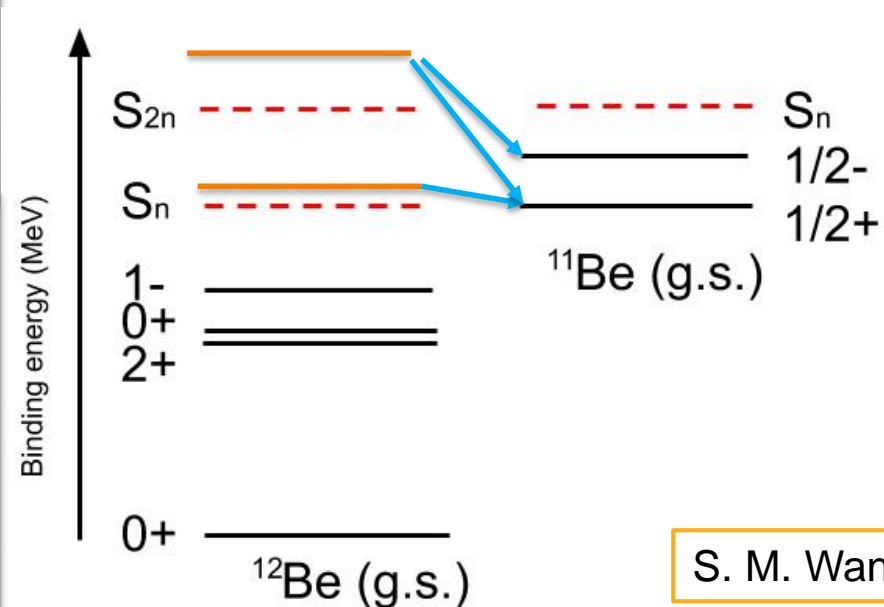


- One state just above the S_n
- One state above the S_{2n} , but has $>80\%$ 1n-decay



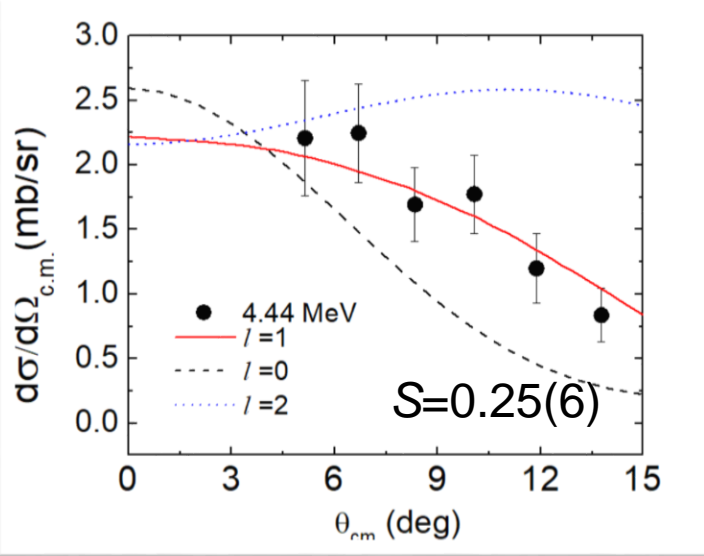
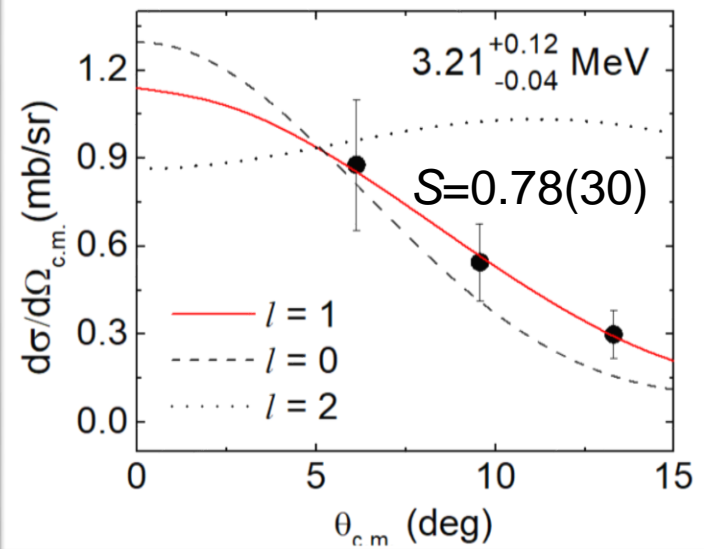
Resonances in ^{12}Be and the role of continuum

- Both are $l=1$, limit the possibility to 0-, 1-, 2-
- Both have a dominant decay branching ratio to $^{11}\text{Be}+n$
- Gamow coupled-channel approach

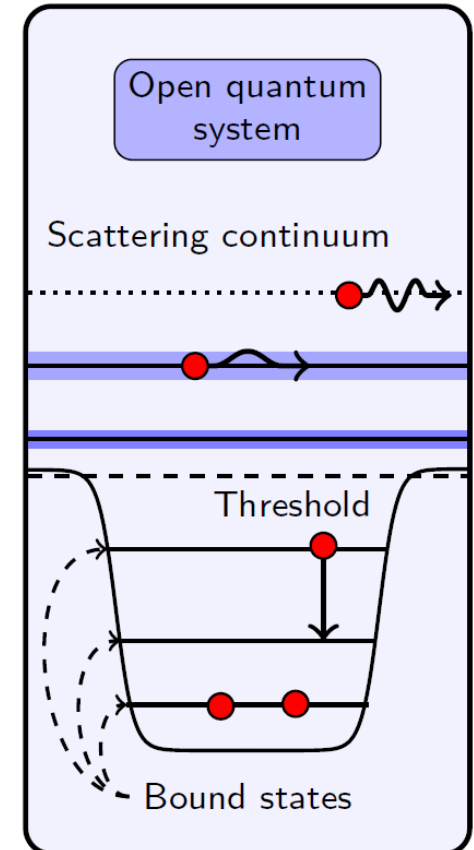
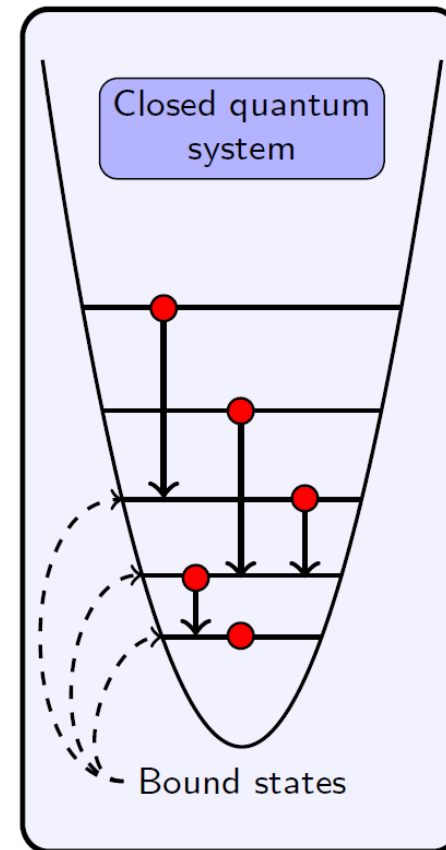
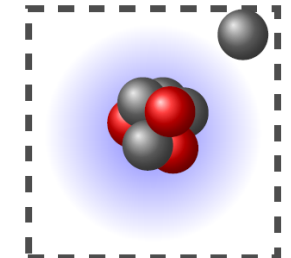
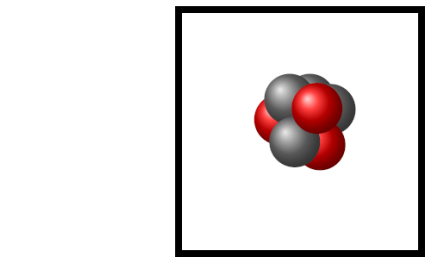
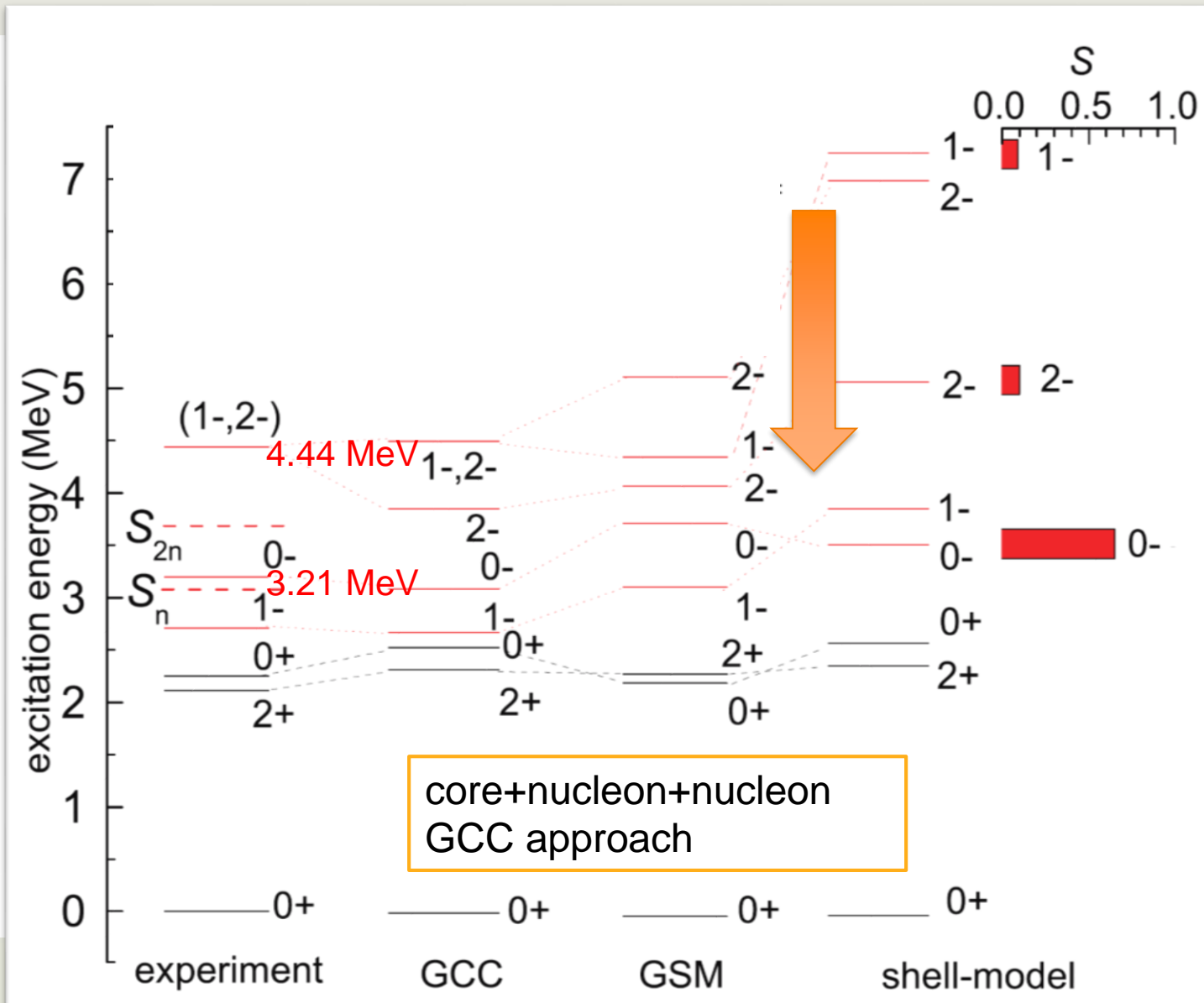


S. M. Wang, *et al.* Phys. Rev. C 99, 054302 (2019)

DWBA calculation by H. T. Fortune
Vincent-Fortune technique

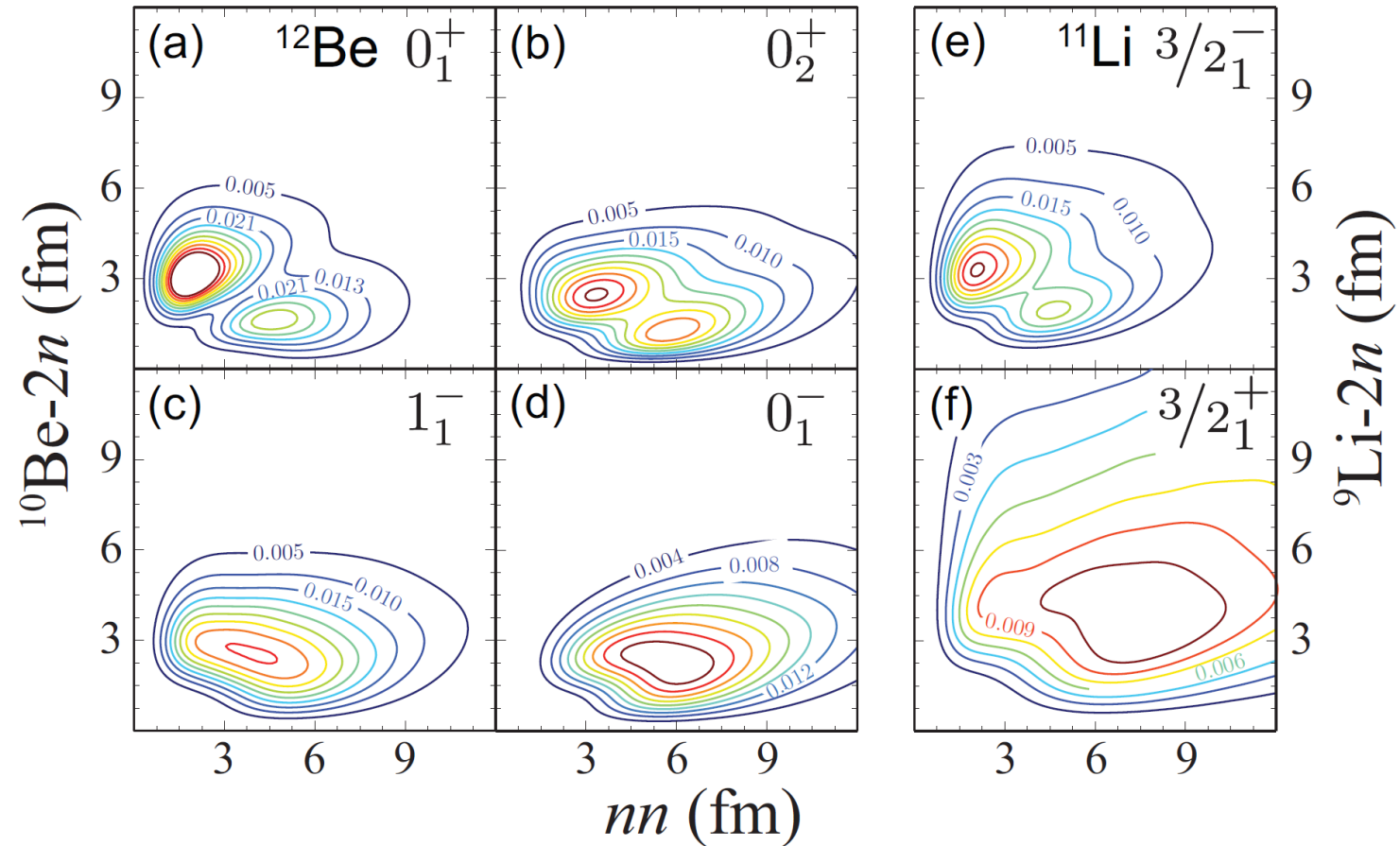


Resonances in ^{12}Be and the role of continuum

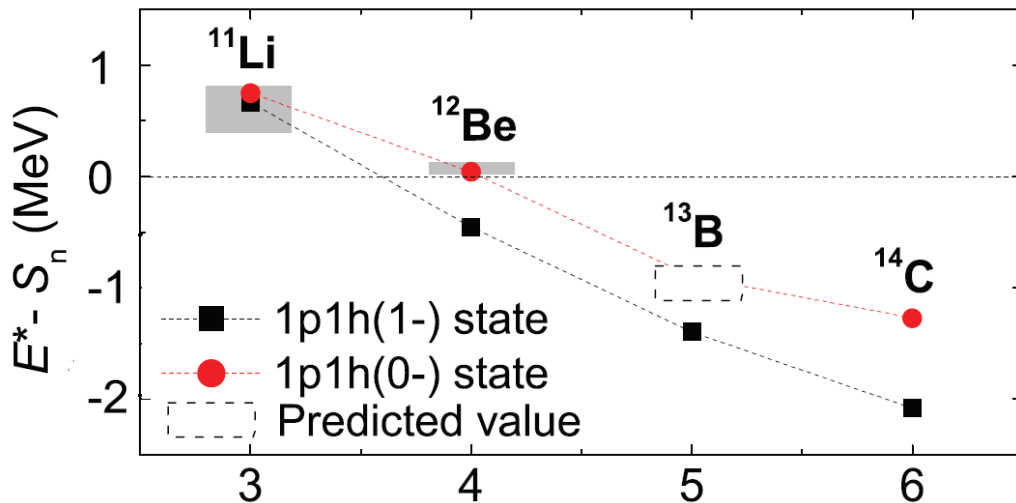


Three-body GCC approach

- Two-nucleon density distributions
- g.s: mixture of a dineutron structure and a cigar-like configuration
- 0_2^+ state: halo structure like the ^{11}Li g.s.
- 0^- and 1_1^- states: two valence neutrons are less correlated



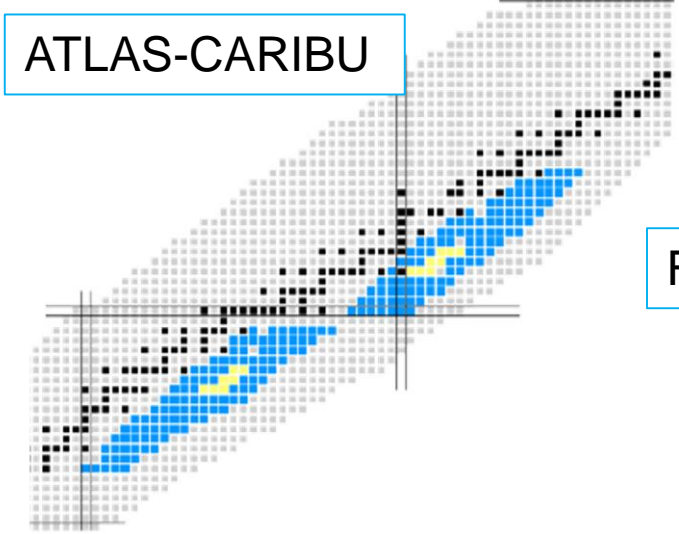
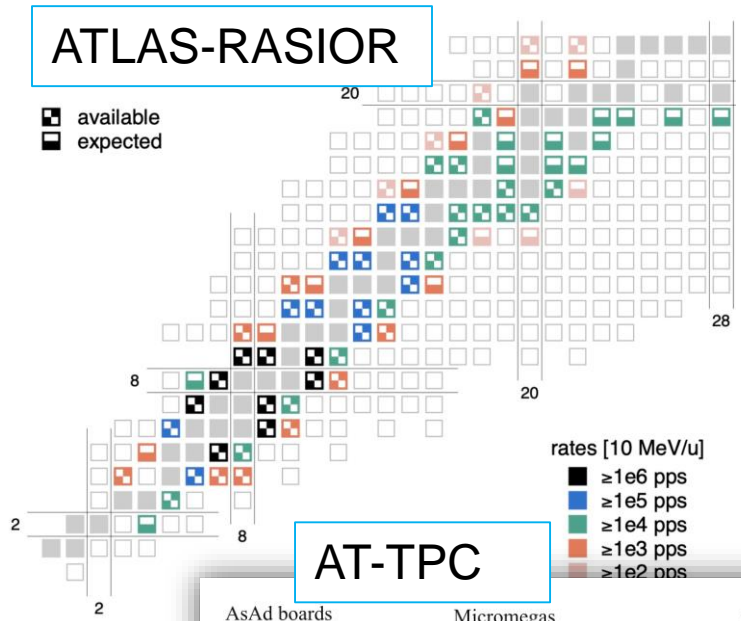
1p-1h resonances in ^{11}Li : experimentally observed dipole resonances



Outline

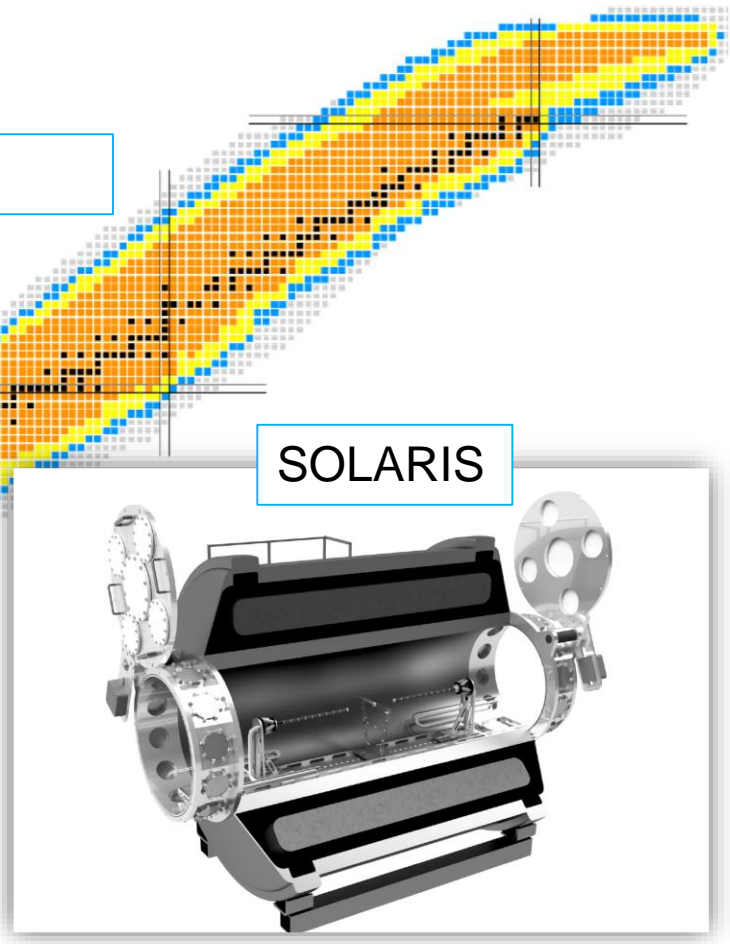
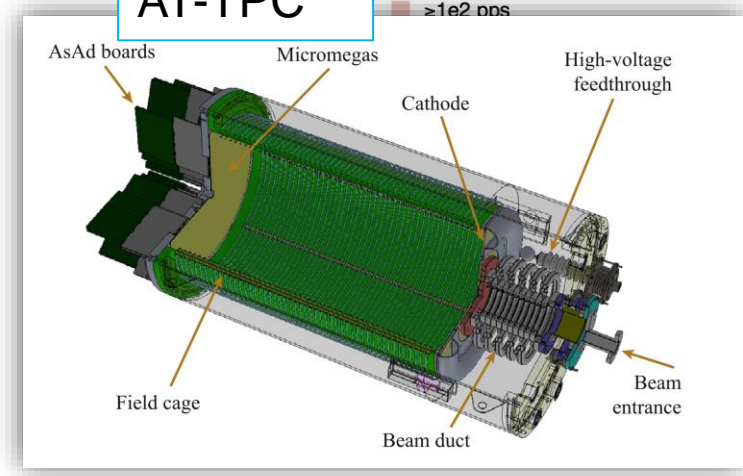
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Instrumentation for transfer reactions

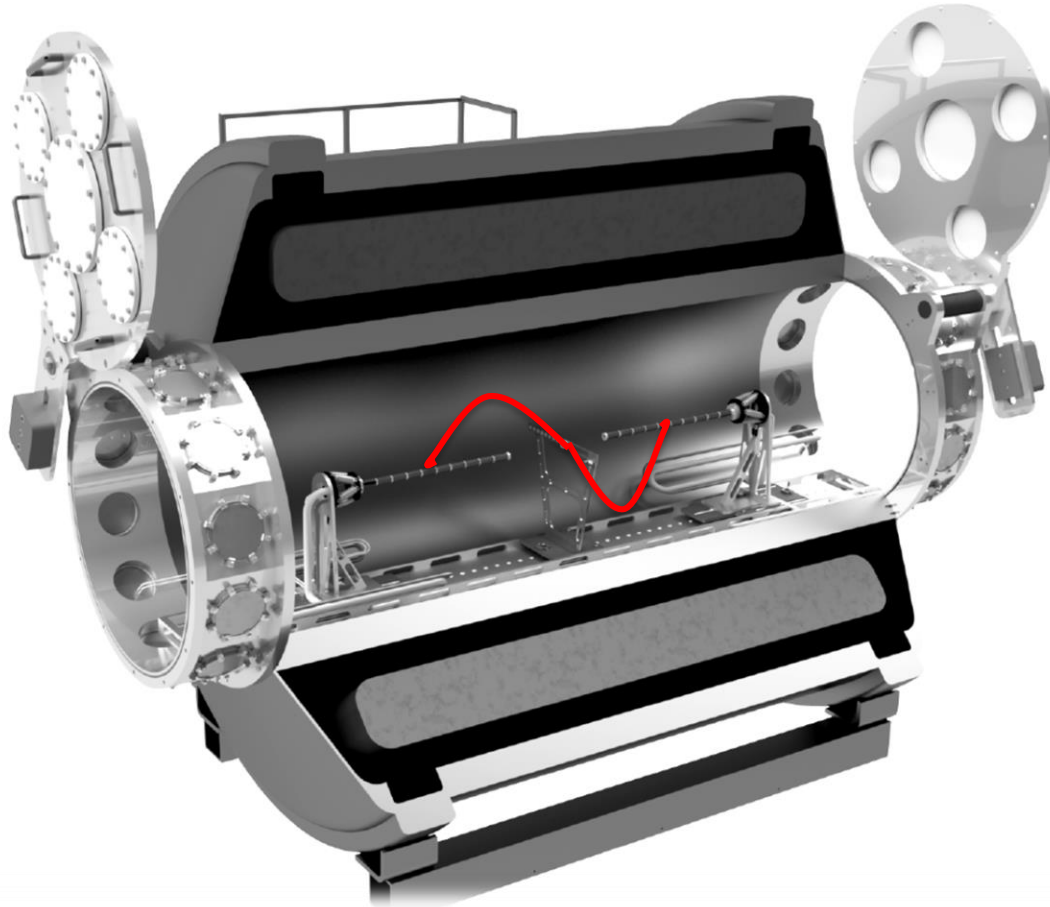


FRIB-ReA

AT-TPC



Instrumentation for transfer reactions

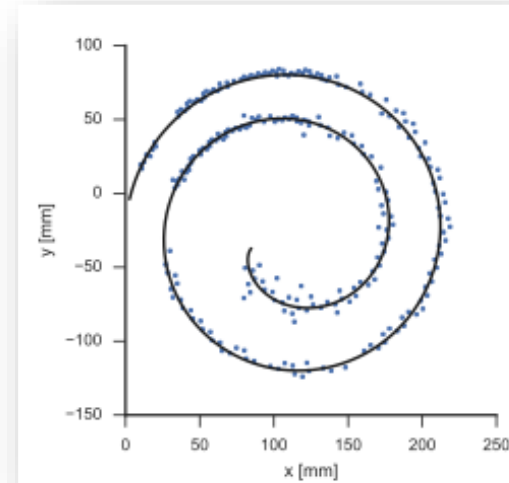
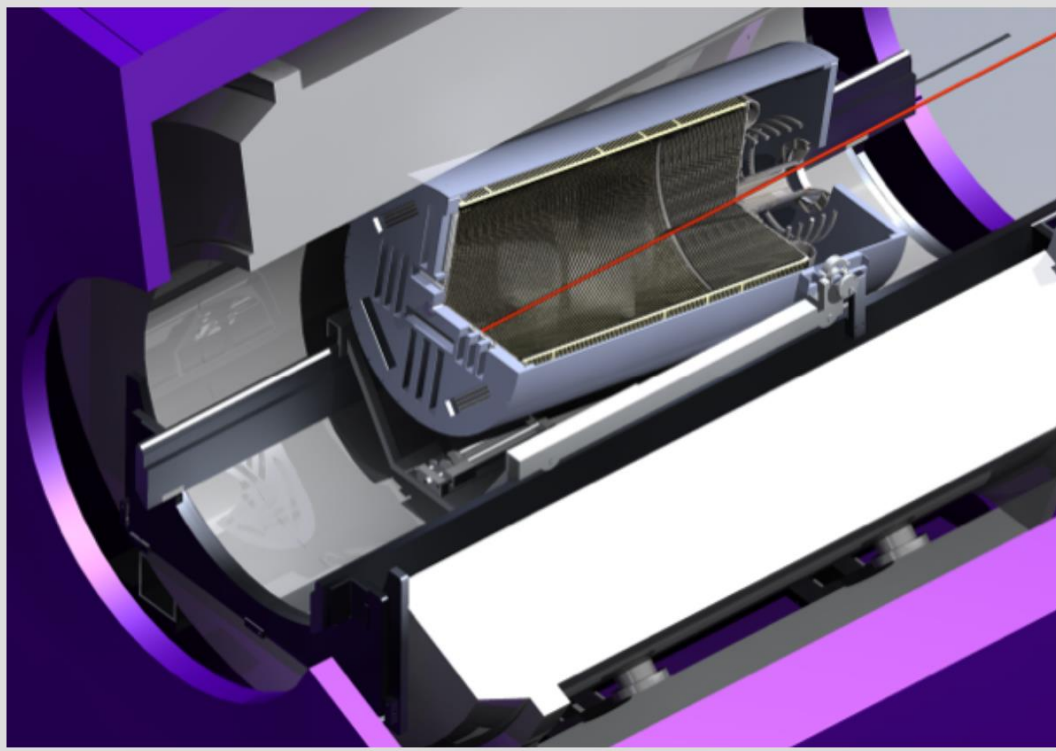


- Similar to Helios
- Measure the reaction with both silicon array upstream and downstream
- Both in AT-TPC and Si-Array modes

SOLARIS White Paper,
<https://www.anl.gov/phy/solaris>.

Instrumentation for transfer reactions

- large-volume gas-filled detector ↔ target isotopes as well as the tracking medium
- a large effective luminosity ↔ beams as low as hundreds of pps
- There has been some resonance scattering measurement with the AT-TPC

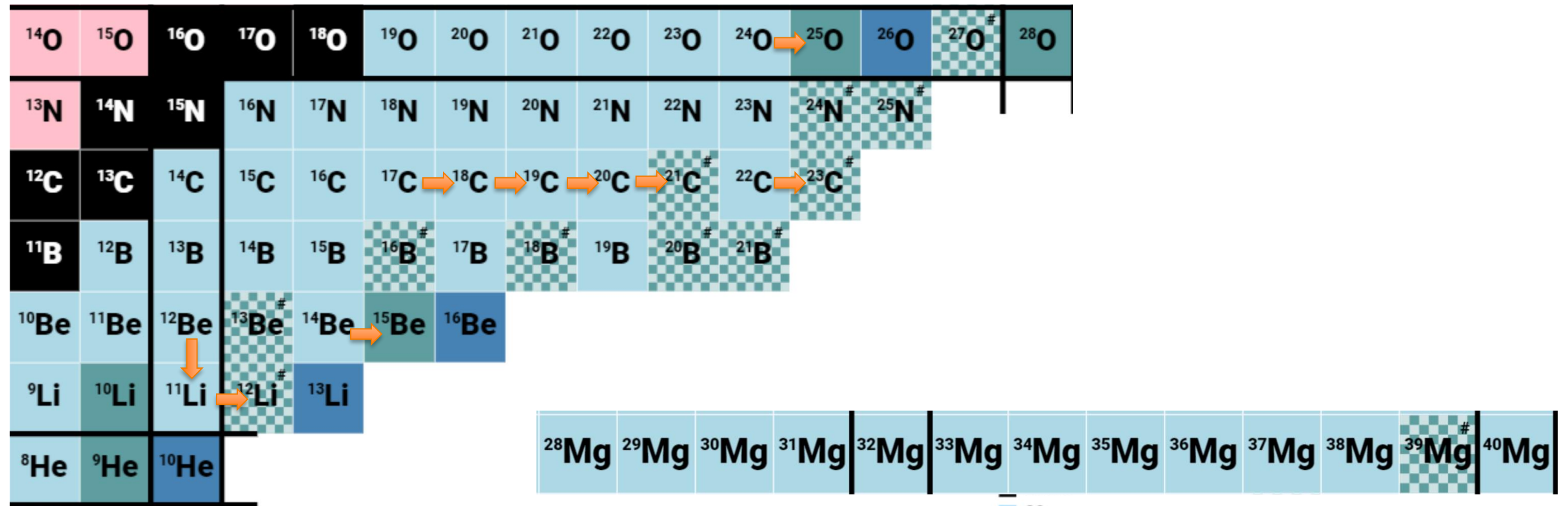


J. Bradt et al., Nucl. Instrum. and Methods in Phys. Res. A 875, 65 (2017)

longer trajectories can be recorded

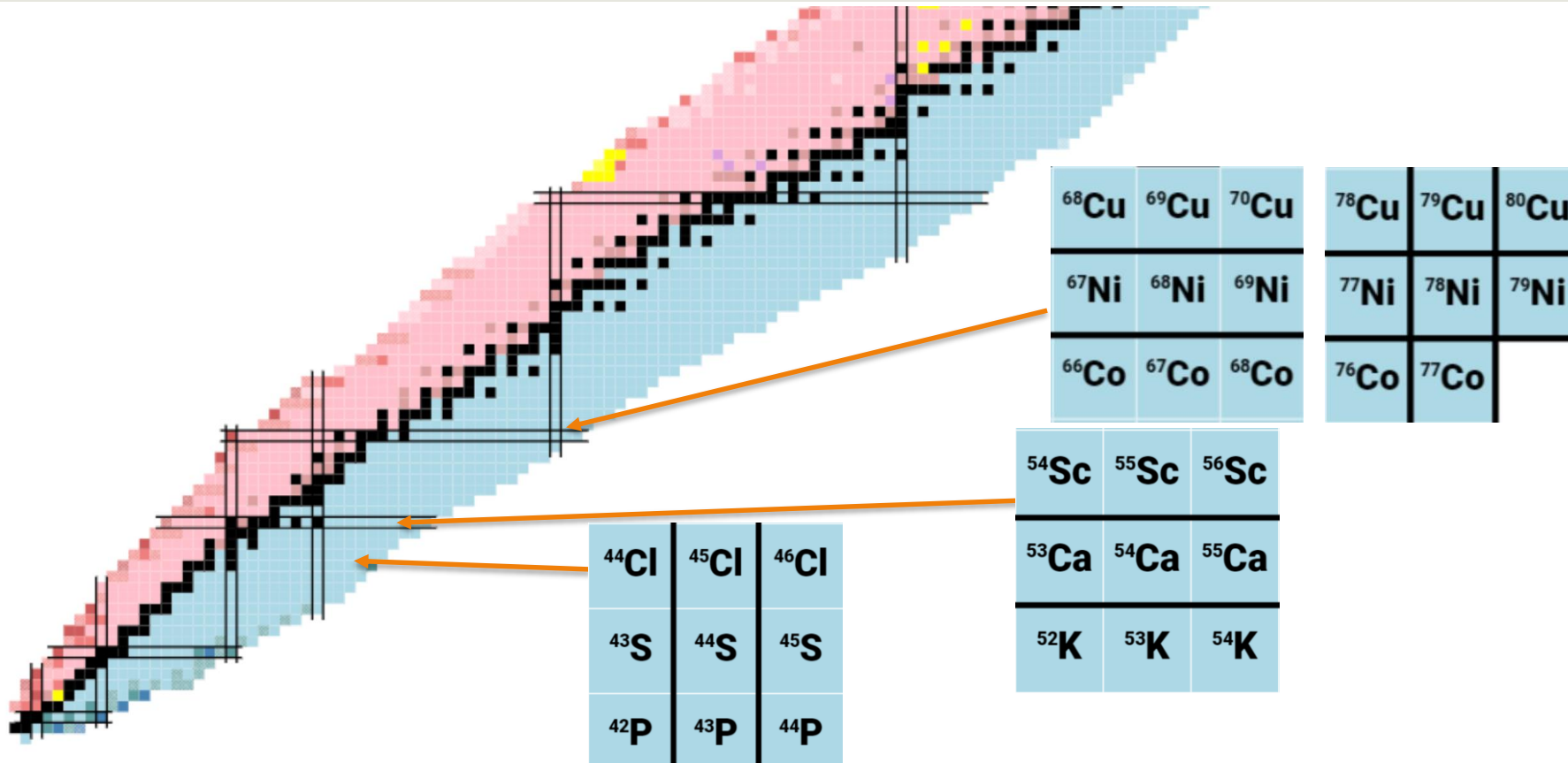
AT-TPC also opens a possible way of the ($^3\text{He}, d$) and (α, t) reaction.

Opportunities with FRIB



- C isotopes—*psd*-shell single-particle structure, $N=14$ and 16 shell decrease
- Mg isotopes—*psdfp*-shell single-particle structure, $N=20$ shell decrease

Opportunities with FRIB

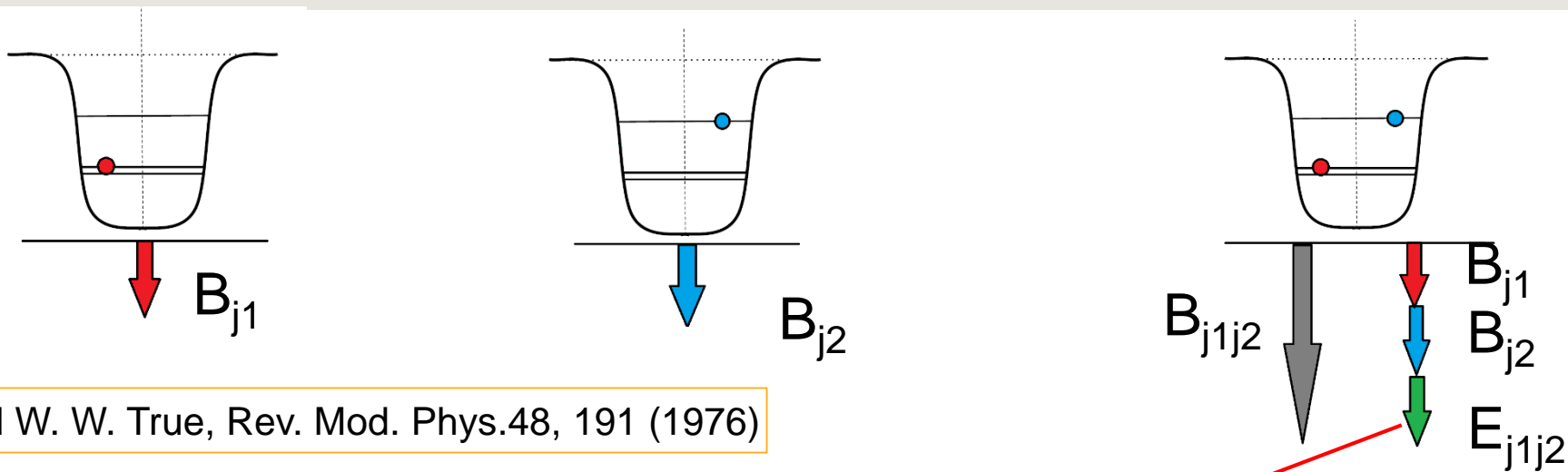


- Ni isotopes—*pf*-shell single-particle structure, above $N = 40, 50$
- Ca isotopes—*pf*-shell single-particle structure, $N = 34$ shell increase

Outline

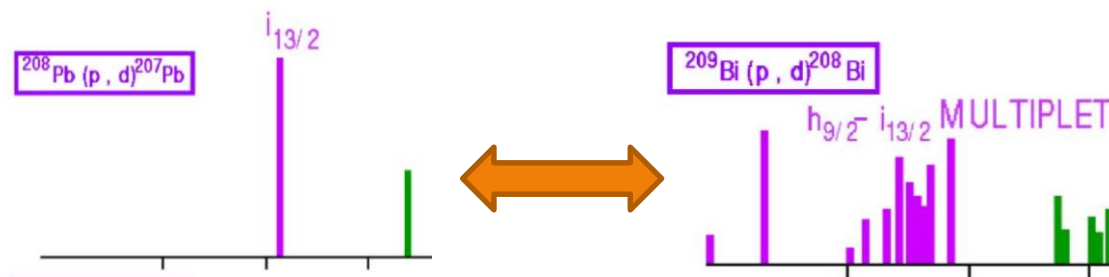
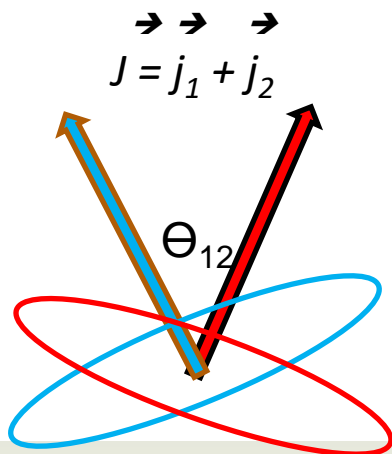
- Overarching questions of nuclear physics
 - Migration of Shell Gaps and Magic Numbers
- Understanding of exotic nuclei ----- Examples: Be isotopes
 - ^{11}Be negative parity states
 - ^{12}Be intruder states and single-particle configuration mixing
- Resonances in weakly-bound nuclei and the role of continuum
 - ^{12}Be resonance with intruder configurations
- Instrumentation for transfer reactions
- Approaching the nuclear force : N-N effective interaction ----- Example: ^{22}F $1d_{5/2}$ -orbital
- Opportunities with FRIB
 - Commissioning of the AT-TPC and SOLARIS using long-lived beams

Approaching the nuclear force : N-N effective interaction



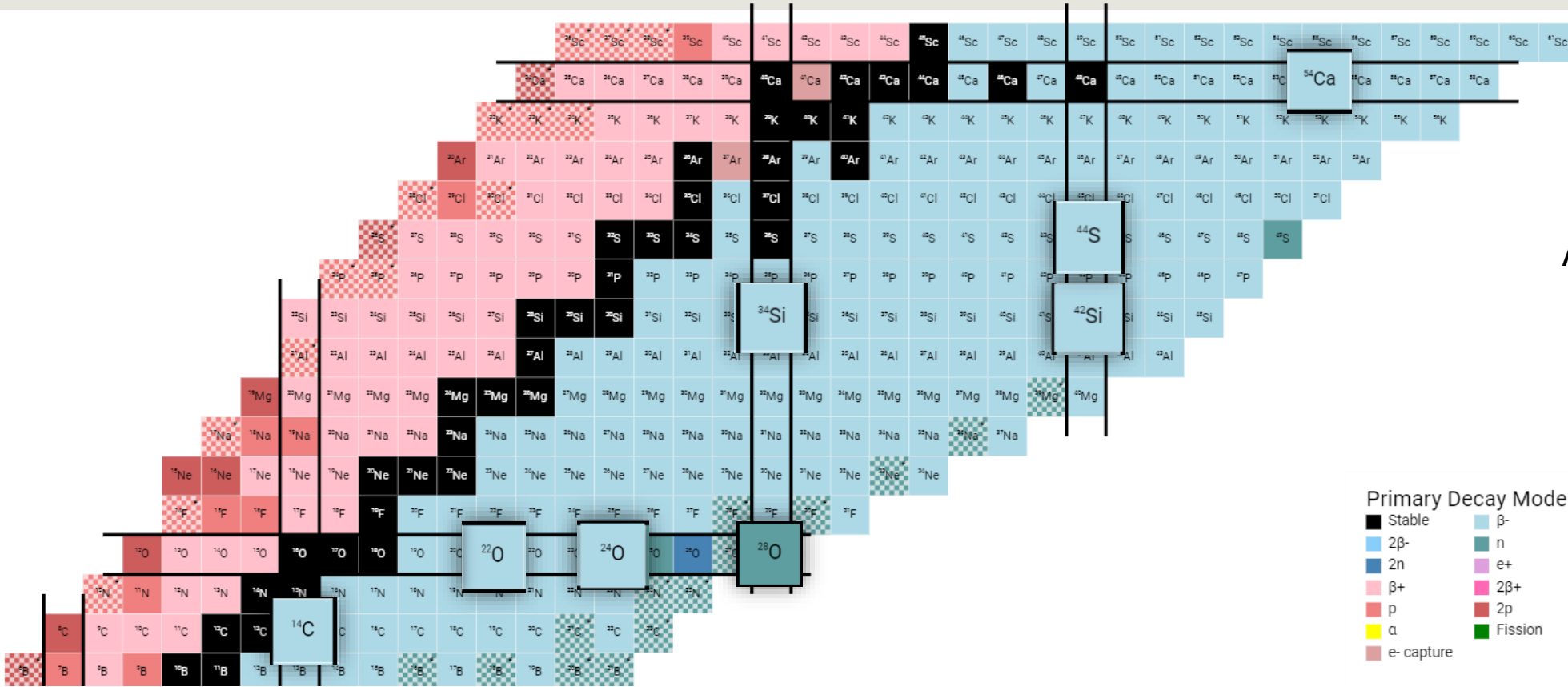
J. P. Schiffer and W. W. True, Rev. Mod. Phys.48, 191 (1976)

Diagonal two-body matrix elements: $E_{j_1j_2} = B_{j_1j_2} - B_{j_1} - B_{j_2}$



example: $j_1 = 5/2, j_2 = 5/2, J = 0 - 5$ multiplets
Average of the multiplets \longrightarrow monopole interaction

Probing nuclear forces in weak-binding system



Available with CARIBU

¹³² Sb	¹³³ Sb	¹³⁴ Sb
¹³¹ Sn	¹³² Sn	¹³³ Sn
¹³⁰ In	¹³¹ In	¹³² In

⁶⁸ Cu	⁶⁹ Cu	⁷⁰ Cu
⁶⁷ Ni	⁶⁸ Ni	⁶⁹ Ni
⁶⁶ Co	⁶⁷ Co	⁶⁸ Co

⁵⁶ Cu	⁵⁷ Cu	⁵⁸ Cu
⁵⁵ Ni	⁵⁶ Ni	⁵⁷ Ni
⁵⁴ Co	⁵⁵ Co	⁵⁶ Co

Primary Decay Mode

- Stable
- β^-
- $2\beta^-$
- β^+
- p
- α
- e-capture
- n
- e+
- $2\beta^+$
- 2p
- Fission

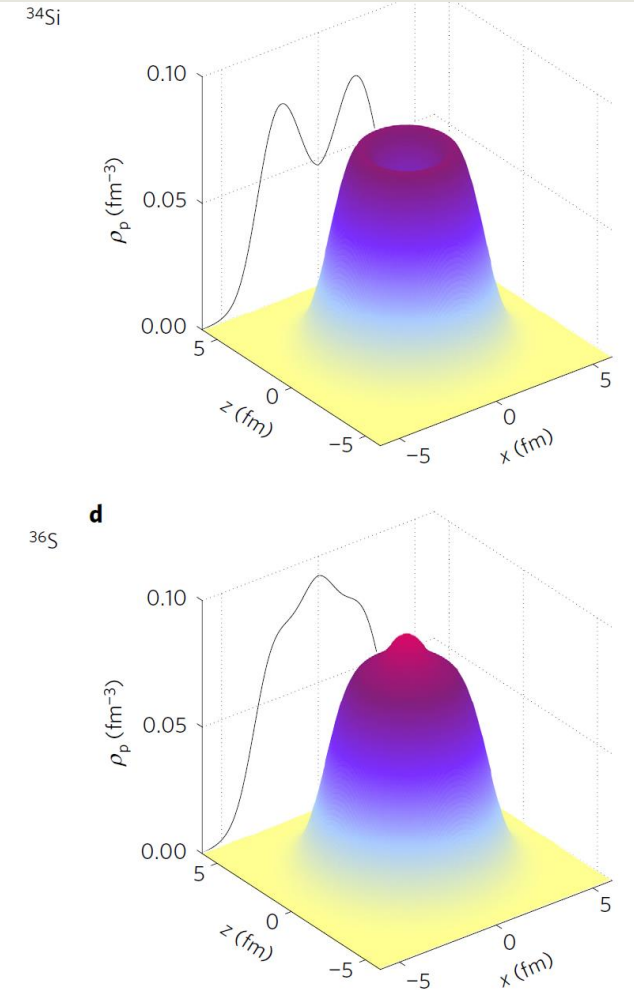
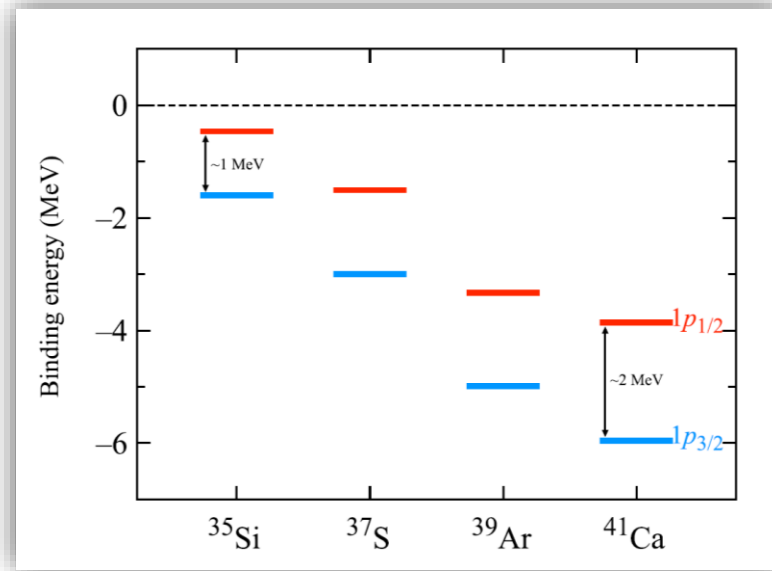
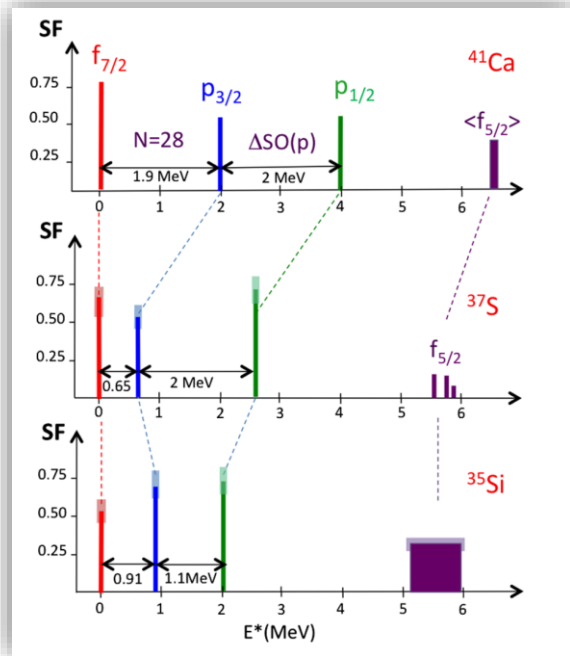
■ FRIB: ²²O, ²⁴O, ⁵⁶Ni, ⁶⁸Ni

■ ²¹O, ²²O and beams around ¹³²Sn will be available using RAISOR and CARIBU

Outline

- Overarching questions of nuclear physics
 - Migration of Shell Gaps and Magic Numbers
- Approaching the nuclear force : N-N effective interaction ----- Example: ^{22}F $1d_{5/2}$ -orbital
- Understanding of exotic nuclei ----- Examples: Be isotopes
 - ^{11}Be negative parity states
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 - Commissioning of the AT-TPC and SOLARIS using long-lived beams

Commissioning of the AT-TPC and SOLARIS using long-lived beams



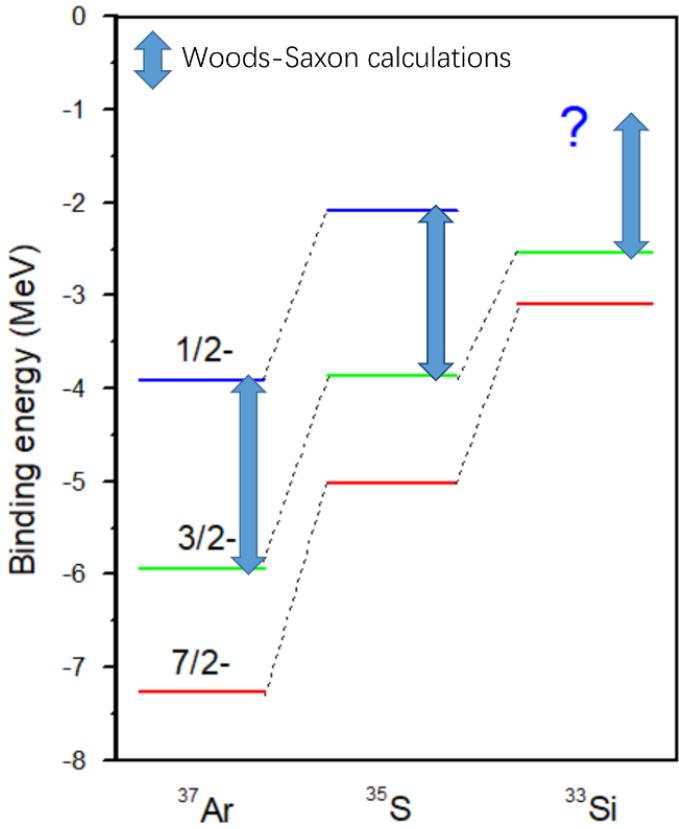
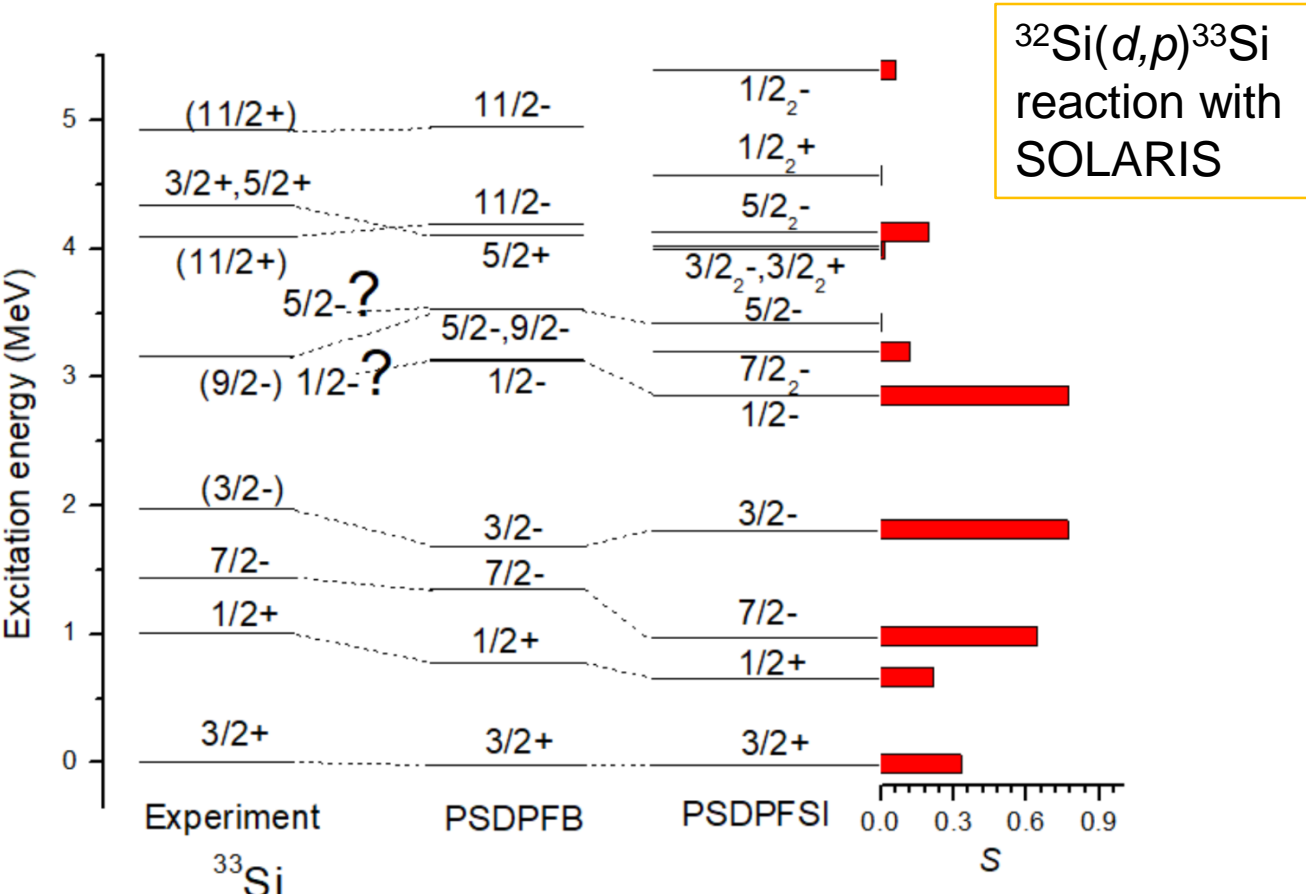
- A similar case can be established by isotonic chain ^{33}Si , ^{35}S , ^{37}Ar
 - What is the trend for the SO-splitting in this case?
 - What is single-particle energies of the orbitals determining the N=20 and N=28 shell gap?
 - Enrich our understanding of the mechanics driving behind
 - Bridge to the nuclei in the island of inversion

A. Mutschler, et al, Nature Physics 13, 155 (2016)

G. Burgunder, et al, Phys. Rev. Lett. 112, 042502 (2014).

B. P. Kay, et al, Phys. Rev. Lett. 119, 182502 (2017).

Commissioning of the AT-TPC and SOLARIS using long-lived beams



Approved by NSCL PAC

Commissioning of the AT-TPC and SOLARIS using long-lived beams

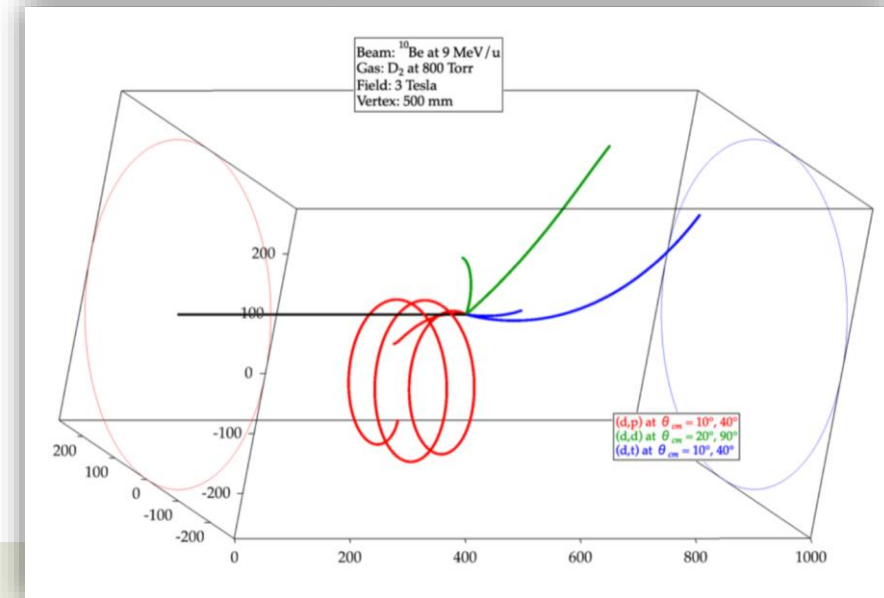
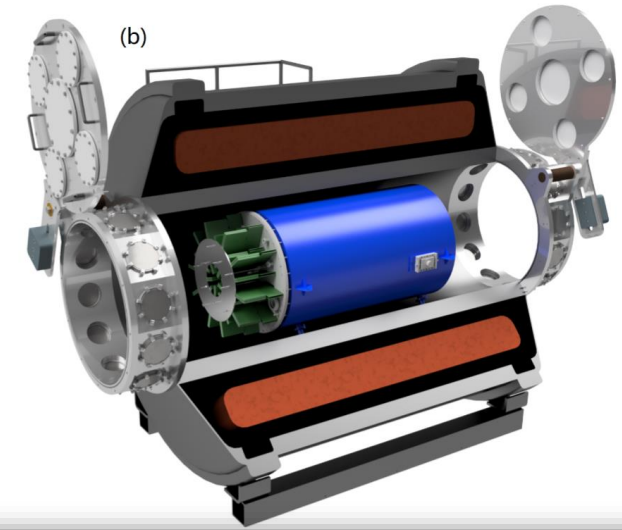
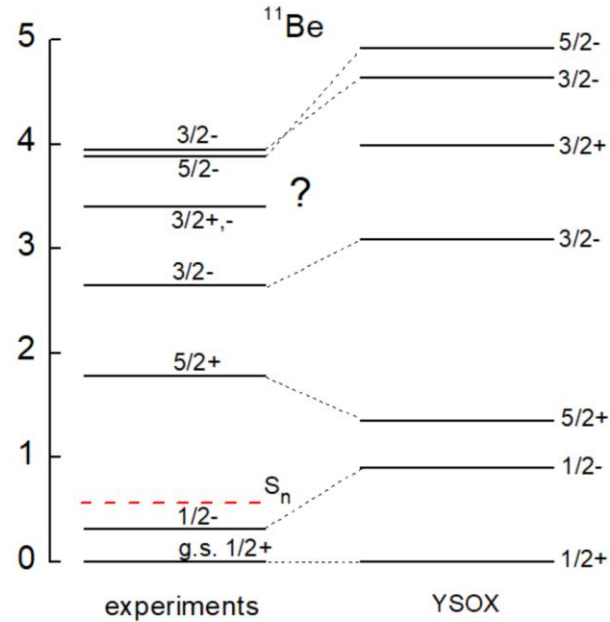
➤ First transfer reaction measurement using the AT-TPC

- Confirm parity of the 3.41-MeV state

➤ Unify the structure and reaction.

- Compare to the calculation within the framework of renormalized nuclear field theory
- Test capability and resolution of AT-TPC for transfer reaction
- Approved by NSCL PAC

F. Barranco, G. Potel, R. A. Broglia, and E. Vigezzi, Phys. Rev. Lett, 119, 082501 (2017)



Summary for the present work

- Overarching questions of nuclear physics:
 - nature of the nuclear force
 - origin of simple patterns
- Testing various theories using ^{11}Be negative parity states
 - *ab-initio* approach (VMC), shell model, Nilsson model
- Determining the cross shell configuration mixing of the two low-lying 0^+ states in ^{12}Be using $^{11}\text{Be}(d,p)^{12}\text{Be}$ reaction.
 - Lowering of d -orbital associated with pairing and deformation
- Testing the role of continuum by measuring unbound state of ^{12}Be .
 - Continuum coupling is essential in ^{12}Be .

New experimental insights on rare nuclei to guide theoretical developments.

Enhance understanding of the nature of weakly-bound nuclei by measurement of exotic and dripline nuclei

Measure resonances in weakly-bound nuclei and test the role of continuum

Summary for the future research plan

- Determine the effective N-N interaction of the $0d_{5/2}$ orbital using $^{21}\text{F}(d,p)^{22}\text{F}$ reaction
 - Probing nuclear forces in weak-binding system
- Commissioning of the AT-TPC and SOLARIS at ReA using the (d,p) reactions on ^{10}Be and ^{32}Si
 - Reduction of the spin-orbital splitting and “bubble nucleus”
- ReA combined with SOLARIS and AT-TPC
 - allows detailed spectroscopic information on key nuclei in the islands of inversion and in isotopic chains of C, Mg, Ca, Ni, and Sn isotopes

Determine shell structure and test configuration interaction theories

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